
**Multifrequency Studies of the Peculiar Quasar 4C +21.35 during the 2010 Flaring Activity**

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MULTIFREQUENCY STUDIES OF THE PECULIAR QUASAR 4C +21.35 DURING THE 2010 FLARING ACTIVITY


( THE FERMI LARGE AREA TELESCOPE COLLABORATION)


( THE MAGIC COLLABORATION)

AND

M. F. Aller71, E. Angelakis72, D. A. Blinov73, S. G. Djorgovski74, A. J. Drake74, N. V. Efimova73,75, M. A. Gurwell76, D. C. Homann77, B. Jordan78, E. N. Kopatskaya75, Y. Y. Kovalev72,79, O. M. Kurtanidze80,81, A. Lähdetömmäki82, V. M. Larionov73,75,86, M. L. Lister83, E. Nieppola82,84, M. G. Nikolashvili80, E. Ros72,85, T. Savolainen7, L. A. Sigua80, AND M. Tornikoski82
1 Deutsches Elektronen-Synchrotron DESY, D-15738 Zeuthen, Germany
2 Space Sciences Laboratory, 7 Gauss Way, University of California, Berkeley, CA 94720-7450, USA
3 W. W. Hansen Experimental Physics Laboratory, Kavli Institute for Particle Astrophysics and Cosmology, Department of Physics and SLAC National Accelerator Laboratory, Stanford University, Stanford, CA 94305, USA
4 Dipartimento di Fisica, Università degli Studi di Perugia, I-06123 Perugia, Italy
5 Istituto Nazionale di Fisica Nucleare, Sezione di Perugia, I-06123 Perugia, Italy
6 Istituto Nazionale di Fisica Nucleare, Sezione di Trieste, I-34127 Trieste, Italy
7 Dipartimento di Fisica, Università di Trieste, I-34127 Trieste, Italy
8 Istituto Nazionale di Fisica Nucleare, Sezione di Padova, I-35131 Padova, Italy
9 Dipartimento di Fisica e Astronomia “G. Galilei,” Università di Padova, I-35131 Padova, Italy
10 Istituto Nazionale di Fisica Nucleare, Sezione di Pisa, I-56127 Pisa, Italy
11 Istituto Nazionale di Fisica Nucleare, Sezione di Trieste, and Università di Trieste, I-34127 Trieste, Italy
12 Dipartimento di Fisica “M. Merlin” dell’Università di Bari and del Politecnico di Bari, I-70126 Bari, Italy
ABSTRACT
The discovery of rapidly variable Very High Energy (VHE; $E > 100$ GeV) $\gamma$-ray emission from 4C +21.35 (PKS 1222+216) by MAGIC on 2010 June 17, triggered by the high activity detected by the Fermi Large Area Telescope (LAT) in high energy (HE; $E > 100$ MeV) $\gamma$-rays, poses intriguing questions on the location of the $\gamma$-ray emitting region in this flat spectrum radio quasar. We present multifrequency data of 4C +21.35 collected from centimeter to VHE during 2010 to investigate the properties of this source and discuss a possible emission model. The first hint of detection at VHE was observed by MAGIC on 2010 May 3, soon after a $\gamma$-ray flare detected by Fermi-LAT that peaked on April 29. The same emission mechanism may therefore be responsible for both the HE and VHE emission during the 2010 flaring episodes. Two optical peaks were detected on 2010 April 20 and June 30, close in time but not simultaneous with the two $\gamma$-ray peaks, while no clear connection was observed between the X-ray and $\gamma$-ray emission. An increasing flux density was observed in radio and mm bands from the beginning of 2009, in accordance with the increasing $\gamma$-ray activity observed by Fermi-LAT, and peaking on 2011 January 27 in the mm regime (230 GHz). We model the spectral energy distributions (SEDs) of 4C +21.35 for the two periods of the VHE detection and a quiescent state, using a one-zone model with the emission coming from a very compact region outside the broad line region. The three SEDs can be fit with a combination of synchrotron self-Compton and external Compton emission of seed photons from a dust torus, changing only the electron distribution parameters between the epochs. The fit of the optical/UV part of the spectrum for 2010 April 29 seems to favor an inner disk radius of $<6$ gravitational radii, as one would expect from a prograde-rotating Kerr black hole.

Key words: galaxies: active – gamma rays: general – quasars: general – quasars: individual (4C +21.35) – radiation mechanisms: non-thermal

Online-only material: color figures

1. INTRODUCTION
In the last few years, flat spectrum radio quasars (FSRQs) have been established as a distinct Very High Energy (VHE) $\gamma$-ray blazar subclass. So far three FSRQs have been detected at $E > 100$ GeV: 3C 279 (Albert et al. 2008), 4C +21.35 (Aleksić et al. 2011), and PKS 1510−089 (Cortina 2012; Abramowicz et al. 2013). These detections were surprising. The VHE emission from FSRQs is expected to be absorbed internally, if emitted within the broad line region (BLR), or externally, for sources located at redshifts where the emission is strongly attenuated by $\gamma\gamma$ pair production via interaction with the Extragalactic Background Light (EBL) photons. In addition, since FSRQs usually have their synchrotron peak at relatively low frequencies (i.e., infrared/optical bands rather than UV/X-ray), their corresponding inverse Compton peak should fall at photon energies less than 1 GeV, and thus a detection at VHE is not expected.

The FSRQ 4C +21.35 (also known as PKS 1222+21) has a redshift of $z = 0.432$ (Osterbrock and Pogge 1987) with a peculiar bent large-scale radio structure (Saikia et al. 1993). Very large apparent superluminal motion ($\beta_{\text{app}} \sim 10$–15) has been detected on milliarcsecond scales for sub-components of the jet (Jorstad et al. 2001; Homan et al. 2001). On the other hand, the ratio of the core-to-extended radio fluxes at GHz frequencies is of the order of unity; thus it is formally a “lobe-dominated quasar” (Kharb & Shastri 2004; Wang et al. 2004).

In GeV $\gamma$-rays, the source was in a quiescent state from the start of the Fermi Gamma-ray Space Telescope mission in 2008 August until 2009 September. After this period, a gradually increasing flux was observed, up to an interval of flaring activity in the first half of 2010. In particular, 4C +21.35 underwent two very strong outbursts in 2010 April and June, observed by the Large Area Telescope (LAT) on board Fermi and composed of several major flares characterized by rise and decay timescales of the order of one day (Tanaka et al. 2011). During the second flaring activity, VHE emission from 4C +21.35 was detected with the MAGIC Cherenkov telescopes on 2010 June 17, with a flux doubling time of about 10 minutes (Aleksić et al. 2011). The simultaneous Fermi-LAT and Major Atmospheric Gamma Imaging Cherenkov (MAGIC) spectrum, corrected for EBL absorption, can be described by a single power law with photon index $\Gamma = 2.72 \pm 0.34$ between 3 GeV and 400 GeV, consistent with emission from a single component in the jet. The absence of a spectral cut-off for $E < 130$ GeV constrains the $\gamma$-ray emission region to lie outside the BLR, which would otherwise absorb the $\approx$10–20 GeV photons by $\gamma\gamma \rightarrow e^+e^-$ production when these $\gamma$-rays pass through the intense circum-nuclear photon fields provided by the BLR itself. At the same time, the rapid VHE variability observed suggests an extremely compact emission region, with size $R \leq c \tau_{\text{var}} \delta_D/(1+z) \sim 10^{15} (\delta_D/80) (\tau_{\text{var}}/10 \text{ minutes})$ cm, where $\tau_{\text{var}}$ is the variability timescale and $\delta_D$ is the Doppler factor. If the blob takes up the entire cross section of the jet, it implies that the emitting region is at a distance $r \sim R/\theta_{\text{open}} \sim 5.7 \times 10^{16} (\delta_D/80) (\tau_{\text{var}}/10 \text{ minutes}) (\theta_{\text{open}}/1 \text{ deg})^{-1}$ cm, where $\theta_{\text{open}}$ is the half-opening angle of the jet. Even for a highly relativistic jet with $\delta_D \sim 100$, the location of the emission region should be well within the BLR.
radius for 4C +21.35, likely $R_{\text{BLR}} \approx 2 \times 10^{17}$ cm (Tanaka et al. 2011).

Different models have been proposed to explain the unusual behavior of 4C +21.35. A very narrow jet can preserve variability at the pc scale, but the likelihood of being in the beam of such a thin jet is small, unless there were many narrow jets, as in a jets-within-jet scenario (Ghisellini & Tavecchio 2008; Giannios et al. 2009; Tavecchio et al. 2011). An alternative model is a compact emission region at the parsec scale responsible for the emission at higher energies, with a second zone either inside or outside the BLR to complete the modeling of the emission at lower energies (Tavecchio et al. 2011). The compact emission sites at the pc scale could be due to self-collimating jet structures (Nalewajko et al. 2012), where the magnetic field dominates the energy density, or to turbulent cells (e.g., Nalewajko et al. 2011; Marscher & Jorstad 2010). Another possibility is that the acceleration of ultra-high energy cosmic rays protons in the inner jet leads to an outflowing beam of neutrons that deposit their energy into ultra-relativistic pairs that radiate VHE synchrotron emission at the parsec scale (Dermer et al. 2012), with associated neutrino production. Even more exotic scenarios have been proposed, such as photons produced inside the BLR, tunneling through it via photon to axion-like particle oscillations (Tavecchio et al. 2012).

In this paper, we present the multifrequency data of 4C +21.35 collected from radio to VHE during 2010, and discuss a possible emission model for this source. A summary of the complete multiwavelength data of 4C +21.35 presented in this paper and the relative facilities can be found in Table 1. The paper is organized as follows. In Sections 2 and 3, we briefly report the LAT and MAGIC data analysis and results, respectively. In Section 4, we report the result of Swift optical/UV/X-ray observations. Optical data collected by the Abastumani, ATOM, Catalina, Crimean, KVA, Steward, and St. Petersburg observatories are presented in Section 5. In Section 6, we present the radio and mm data collected by the Medicina, UMRAO, MOJAVE, OVRO, F-GAMMA, Metsähovi, and SMA facilities. In Section 7, we discuss the light curves behavior and the spectral energy distribution (SED) modeling of three different epochs, and finally we draw our conclusions in Section 8.

Throughout the paper, a $\Lambda$ CDM cosmology with $H_0 = 71 \text{ km s}^{-1} \text{Mpc}^{-1}$, $\Omega_{\Lambda} = 0.73$, and $\Omega_m = 0.27$ is adopted. The corresponding luminosity distance at $z = 0.432$ is $d_L$ = 2370 Mpc, and 1 arcsec corresponds to a projected size of 5.6 kpc.

## 2. MAGIC DATA AND ANALYSIS

The MAGIC experiment is situated in the Observatorio del Roque de los Muchachos in the Canary Island of La Palma (28°45’ north, 18°54’ west), 2200 m above sea level. It consists of two 17 m Imaging Atmospheric Cherenkov Telescopes and can reach an energy threshold as low as 50 GeV in standard trigger mode. Details on the performance of the MAGIC telescope stereo system can be found in Aleksic et al. (2012).

MAGIC observed 4C +21.35 between 2010 May 3 and June 19. In total, 16 hr of good-quality data were collected. The data analysis was performed in the MAGIC Analysis and Reconstruction Software analysis framework (Moralejo et al. 2011). On May 3 (MJD 55319), MAGIC observed 4C +21.35 with a signal significance of 10.2 by Atwood et al. (2009).

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None of the other nights showed a statistically significant excess of signal over the background. Upper limits at 95% C.L. were calculated above 150 GeV assuming a power law with the same photon index measured on June 17 (i.e., $\Gamma_{\gamma} = 3.75$) for the nights between May 5 and June 13. The rest of the nights were not included in the upper limit calculation due to strong moonlight constraints. The upper limits range between 1.4% C.U. (on June 12; MJD 55359), as reported in Table 2. Considering the period from May 5 to June 13 (total time: 12.5 hr) an upper limit of 1.6% C.U. was estimated.

## 3. FERMI-LAT

The Fermi-LAT is a $\gamma$-ray telescope operating from 20 MeV to above 300 GeV. The LAT has a large peak effective area ($\sim$8000 cm$^2$ for 1 GeV photons), a relative energy resolution typically $\sim$10%, and a field of view of about 2.4 sr with an angular resolution (68% containment angle) better than 1° for energies above 1 GeV. Further details about the LAT are given by Atwood et al. (2009).
Table 2
Daily Upper Limits Estimated by MAGIC for $E > 150$ GeV
Assuming a Spectrum Slope 3.7

<table>
<thead>
<tr>
<th>Date (UT)</th>
<th>Effective Time (hr)</th>
<th>Integral Limit (cm$^{-2}$ s$^{-1}$) above 150 GeV</th>
<th>Integral Limit (in MAGIC C.U.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2010 May 5</td>
<td>0.5</td>
<td>1.2e-11</td>
<td>3.7%</td>
</tr>
<tr>
<td>2010 May 6</td>
<td>0.7</td>
<td>1.1e-11</td>
<td>3.3%</td>
</tr>
<tr>
<td>2010 May 7</td>
<td>0.8</td>
<td>1.8e-11</td>
<td>5.5%</td>
</tr>
<tr>
<td>2010 May 8</td>
<td>1.4</td>
<td>1.7e-11</td>
<td>5.4%</td>
</tr>
<tr>
<td>2010 May 30</td>
<td>0.9</td>
<td>4.6e-12</td>
<td>1.4%</td>
</tr>
<tr>
<td>2010 May 31</td>
<td>1.0</td>
<td>2.6e-11</td>
<td>8.1%</td>
</tr>
<tr>
<td>2010 Jun 1</td>
<td>1.2</td>
<td>5.1e-12</td>
<td>1.6%</td>
</tr>
<tr>
<td>2010 Jun 2</td>
<td>0.9</td>
<td>1.0e-12</td>
<td>3.7%</td>
</tr>
<tr>
<td>2010 Jun 3</td>
<td>1.1</td>
<td>8.4e-12</td>
<td>2.6%</td>
</tr>
<tr>
<td>2010 Jun 4</td>
<td>1.2</td>
<td>8.0e-12</td>
<td>2.5%</td>
</tr>
<tr>
<td>2010 Jun 6</td>
<td>1.0</td>
<td>1.4e-11</td>
<td>4.3%</td>
</tr>
<tr>
<td>2010 Jun 7</td>
<td>0.6</td>
<td>2.1e-11</td>
<td>6.4%</td>
</tr>
<tr>
<td>2010 Jun 8</td>
<td>0.7</td>
<td>1.3e-11</td>
<td>4.0%</td>
</tr>
<tr>
<td>2010 Jun 9</td>
<td>0.9</td>
<td>2.4e-11</td>
<td>7.3%</td>
</tr>
<tr>
<td>2010 Jun 12</td>
<td>0.6</td>
<td>4.1e-11</td>
<td>12.7%</td>
</tr>
<tr>
<td>2010 Jun 13</td>
<td>0.6</td>
<td>2.5e-11</td>
<td>7.8%</td>
</tr>
</tbody>
</table>

Very strong GeV flares from 4C +21.35 were detected by Fermi-LAT in 2010 April and June, with spectra characterized by a broken power law with spectral breaks near 1–3 GeV photon energies and a photon index after the break $\sim 2.4$. In contrast, the quiescent state observed by the LAT during 2008 August–2009 September has been fit by a single power law with photon index $\Gamma_y = 2.57 \pm 0.07$. All details of the LAT analysis for that period were presented in Tanaka et al. (2011). After the 2010 flaring period, a decreasing $\gamma$-ray activity of 4C +21.35 was observed by Fermi-LAT, and then in mid-2011 the source faded back into a quiescent state.96 4C +21.35 is found in the first Fermi hard source list (1FHL) as 1FHL J1224.8+2122 (Ackermann et al. 2013). This object is the most variable source in the 1FHL catalog.

4. SWIFT OBSERVATIONS

The Swift satellite (Gehrels et al. 2004) performed 28 observations of 4C +21.35 between 2010 February 12 and June 23. The observations were performed with all three onboard instruments: the Burst Alert Telescope (BAT; Barthelmy et al. 2005, 15–150 keV), the X-ray Telescope (XRT; Burrows et al. 2005, 0.2–10.0 keV), and the UltraViolet Optical Telescope (UVOT; Roming et al. 2005, 170–600 nm).

4.1. Swift/BAT

4C +21.35 is detected in the BAT 70 month catalog, generated from the all-sky survey in the time period 2004 November–2010 August. The data reduction and extraction procedure of the 8 channel spectrum is described in Baumgartner et al. (2013). The 14–195 keV spectrum is well described by a power-law with photon index of 1.76$^{+0.25}_{-0.23}$ ($\chi^2_{red} = 0.60$, 6 d.o.f.). The resulting unabsorbed 14–195 keV flux is $(2.2 \pm 0.4) \times 10^{-11}$ erg cm$^{-2}$ s$^{-1}$. No significant variability was observed in the BAT light curve on monthly time scales. Nevertheless, the hard X-ray flux of this source is below the sensitivity of the BAT instrument for the short exposure times of single Swift observations.

4.2. Swift/XRT

The XRT data were processed with standard procedures (xrtpipeline v0.12.6), filtering, and screening criteria by using the HEASoft package (v6.11). The data were collected in photon counting mode in all observations, and only XRT event grades 0–12 were selected. The source count rate was low ($<0.5$ counts s$^{-1}$), thus pile-up correction was not required. Data collected in the same day were summed in order to have better statistics. Since the observation performed on 2010 May 26 was short ($\sim500$ s), it was not considered. Source events were extracted from a circular region with a radius of 20 pixels (1 pixel = 2.36), while background events were extracted from a circular region with radius of 50 pixels away from the source region. Ancillary response files were generated with xrtmkarf, and account for different extraction regions, vignetting and point-spread function corrections. When the number of photons collected was smaller than 200, the Cash statistic was used (Cash 1979).

We fit the spectra for all the individual Swift observations with an absorbed power law with a neutral hydrogen column density fixed to its Galactic value ($N_H = 2.09 \times 10^{20}$ cm$^{-2}$; Kalberla et al. 2005). The X-ray light curve and spectral shape derived from these fits is discussed in Section 7.1 together with the other multiwavelength data.

4.3. Swift/UVOT

The script that handles the UVOT analysis is uvotgrblc (available within HEASoft). It determines the aperture corrected magnitude by (1) selecting the aperture size based on the observed source count rate and the presence of close field sources; (2) choosing the background region based on the surface brightness among three annular regions centered on the main source in the summed images (circular regions around field sources are automatically excluded); (3) finding field stars to estimate the aperture correction, specific for each observation; and (4) calling the task uvotsource to estimate the photometry.

Since 4C +21.35 is a very bright object in the optical and UV range and lies in a sparsely populated area of the sky, uvotgrblc selected a circle of $5''$ as the source extraction region and a full annulus for the background region for all the observations. The typical inner/outer radii for the background regions were 27$/''$35 and 35$/''$42. The UVOT magnitudes during these observations showed ranges as follows: $v = 15.67–15.21$, $b = 15.65–15.43$, $u = 14.67–14.34$, $w1 = 14.37–14.08$, $m2 = 14.25–13.90$, $w2 = 14.16–13.90$, with a typical error of 0.06 mag. As discussed in detail in Section 7.1, no significant increase in flux was observed by UVOT during 2010 February–June, but the sparse coverage does not allow us to draw firm conclusions.

5. OPTICAL OBSERVATIONS

In this section, we briefly describe the programs performing optical observations of 4C +21.35 and the corresponding data analysis. These optical data are discussed together with the multiwavelength data in Section 7.1.

5.1. Abastumani, Crimean and St. Petersburg Data

Observational data at optical wavelengths (R band) were obtained at the 0.7 m reflector of the Crimean Astrophysical Observatory and 0.4 m LX-200 telescope of the Astronomical Institute of St. Petersburg State University, both equipped with

96 http://fermi.gsfc.nasa.gov/FTP/glast/data/lat/catalogs/asp/current/lightcurves/PKSB1222+216_86400.png
photo polarimeters based on ST-7XME CCDs. A standard technique of bias and dark subtraction and flat-field correction was used. Photometric calibration was made relative to two nearby standard stars, located in the same field.

Optical observations in $R$-band were performed also by the 0.7 m meniscus $f/3$ telescope of Abastumani Astrophysical Observatory in Abastumani, Georgia.

5.2. ATOM Data

Optical observations in $R$ filter for this campaign were obtained between 2010 February and May with the 0.8 m optical telescope ATOM in Namibia (Hauser et al. 2004). ATOM is operated robotically by the H.E.S.S. collaboration and obtains automatic observations of confirmed or potential $\gamma$-bright blazars. Data analysis (debiasing, flat fielding, and photometry with Source-Extractor; Bertin and Arnouts 1996) is conducted automatically using the pipeline developed by the ATOM Team.

5.3. Catalina Real-Time Transient Survey

The source is monitored by the Catalina Real-Time Transient Survey (CRTS; http://crts.caltech.edu; Drake et al. 2009; Djorgovski et al. 2011), using the 0.68 m Schmidt telescope at Catalina Station, AZ, and an unfiltered CCD. The typical cadence is to obtain four exposures separated by 10 minutes in a given night; this may be repeated up to four times per lunar, over a period of $\sim$6–7 months each year, while the field is observable. Photometry is obtained using the standard Source-Extractor package (Bertin and Arnouts 1996), and roughly calibrated to the $V$ band in terms of the magnitude zero point. The light curve, accessible through the CRTS Web site and spanning $\sim$six yr, shows a dramatic increase in optical variability of this source starting in late 2009.

5.4. KVA Data

The KVA (Kungliga Vetenskaps Akademiekehrlobservatorium) is located on Roque de los Muchachos, La Palma (Canary Islands), and is operated by the Tuorla Observatory, Finland (http://users.utu.fi/kani/1m). The telescope consists of a 0.6 m $f/15$ Cassegrain devoted to polarimetry, and a 0.35 m $f/11$ SCT auxiliary telescope for multicolor photometry. The telescope has been successfully operated remotely since autumn 2003. The KVA is used for optical support observations for MAGIC by making $R$-band photometric observations, typically one measurement per night per source. The data were reduced by the Tuorla Observatory Team as described in K. Nilsson et al. (in preparation).

5.5. Steward Observatory

4C +21.35 was systematically monitored by Steward Observatory during the Fermi observations, providing spectropolarimetry and spectrophotometry measurements of this object in $V$ band, as reported also in Smith et al. (2011). Figure 1 shows the behavior of the observed degree of optical polarization $P$, and the position angle of the polarization vector $\Theta$ as a function of time. Visual inspection of the plot seems to show that in general periods of high flux correspond to periods of relatively high polarization degree and only small rotation of the polarization angle vector. In particular, a marginal increase of polarization degree but no significant rotation of the polarization angle was observed in 2010 June, during the period of HE and VHE flaring activity.

Spectrophotometry during 2010–2011 did not show significant changes in the flux of the broad Mg $\text{II} \lambda 2800$ and Balmer emission lines despite large optical continuum variation. This indicates that non-thermal emission from the jet has a negligible influence on the BLR lines fluxes. Smith et al. (2011) suggested that the beaming jet emission intersects only a small fraction of the volume containing the emission-line gas. A different behavior was observed in 3C 454.3, with a significant increase of the Mg $\text{II}$ emission line flux during the optical and $\gamma$-ray flaring activity in 2010 November. This event occurred after a mm flare onset, during an increase in the optical polarization percentage, and before the emergence of a superluminal knot from the radio core. This suggests the presence of BLR clouds surrounding the radio core in 3C 454.3 (Leon-Tavares et al. 2013).

6. RADIO AND MM OBSERVATIONS

In this section, we present the radio and mm light curves and spectra of 4C +21.35 collected between 2009 January 1 and 2011 February 28 to investigate their connection with the $\gamma$-ray activity. The data collected between 230 GHz and 5 GHz are reported in Figure 2 and discussed in detail in Section 7.1. In addition we studied the radio structure and jet kinematics of this source during the MOJAVE monitoring observations.

6.1. SMA Data

The 230 GHz (1.3 mm) light curve was obtained at the Submillimeter Array (SMA) on Mauna Kea (Hawaii). 4C +21.35 is included in an ongoing monitoring program at the SMA to determine the fluxes of compact extragalactic radio sources that can be used as calibrators at mm wavelengths. Details of the observations and data reduction can be found in Gurwell et al. (2007).
Figure 2. Radio and mm light curves of 4C +21.35 in units of Jy. The period covered is between 2009 January 1 (MJD 54837) and 2011 February 28 (MJD 55620). The data are collected (from top to bottom panel) by SMA at 230 GHz (circles), IRAM at 142 GHz (squares) and 86 GHz (triangles); Metsähovi at 37 GHz (circles) and Effelsberg at 32 GHz (squares); Effelsberg at 23 GHz (circles) and Medicina a 22 GHz (squares); OVRO (circles), UMRAO (squares), Effelsberg (triangles) at 15 GHz; Effelsberg (circles) and UMRAO (squares) at 8 GHz; Effelsberg (circles), Medicina (squares), and UMRAO (triangles) at 5 GHz. For clarity, errors are not shown when <5%.

Data from this program are updated regularly and are available at the SMA Web site.98

6.2. F-GAMMA Project

Radio spectra and light curves of 4C +21.35 were obtained within the framework of a Fermi-related monitoring program of γ-ray blazars (F-GAMMA project; Fuhrmann et al. 2007). The frequency range spans 2.64 GHz to 142 GHz using the Effelsberg 100 m and IRAM 30 m telescopes. The Effelsberg measurements were conducted with the secondary focus heterodyne receivers at 2.64, 4.85, 8.35, 10.45, 14.60, 23.05, 32.00, and 43 GHz. The observations were performed quasimultaneously with cross-scans, that is, slewing over the source position, in azimuth and elevation directions, with adaptive numbers of sub-scans for reaching the desired sensitivity (for details, see Fuhrmann et al. 2008; Angelakis et al. 2008). Pointing offset correction, gain correction, atmospheric opacity correction, and sensitivity correction have been applied to the data. The IRAM 30 m observations were carried out with calibrated cross-scans using the EMIR horizontal and vertical polarization receivers operating at 86.2 and 142.3 GHz. The opacity-corrected intensities were converted into the standard temperature scale and finally corrected for small remaining pointing offsets and systematic gain-elevation effects. The conversion to the standard flux density scale was done using the instantaneous conversion factors derived from frequently observed primary (Mars, Uranus) and secondary (W3(OH), K350A, NGC 7027) calibrators. The radio spectra from 2.64 GHz to 43 GHz obtained during five epochs of Effelsberg observations between 2009 January 24 and 2011 April 29 are shown in Figure 3. A significant increase of the flux density has been observed from 2009 May to September at 43 GHz, while at longer wavelengths the increase occurs later, likely due to synchrotron self-absorption opacity effects. This time difference led to a significant radio spectral evolution, possibly related to the activity observed in γ-rays.

6.3. Metsähovi Data

The 37 GHz observations were made with the 13.7 m diameter Metsähovi radio telescope, which is a radome enclosed paraboloid antenna situated in Finland (24°23′38″E, +60°13′05″). The measurements were made with a 1 GHz-band dual beam receiver centered at 36.8 GHz. The HEMPT (high electron mobility pseudomorphic transistor) front end operates at room temperature. The observations were taken with an ON–ON technique, alternating the source and the sky in each feed horn. A typical integration time to obtain one flux density data point is between 1200 and 1400 s. The detection limit of the telescope at 37 GHz is on the order of 0.2 Jy under optimal conditions. Data points with a signal-to-noise ratio <4 are treated as nondetecteds. The flux density scale is set by observations of thermal radio source DR 21. Sources NGC 7027, 3C 274, and 3C 84 are used as secondary calibrators. A detailed description of the data reduction and analysis is given in Teräsranta et al. (1998). The error estimate in the flux density includes the contribution from the measurement rms and the uncertainty of the absolute calibration.

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6.4. OVRO Data

As part of an ongoing blazar monitoring program, the Owens Valley Radio Observatory (OVRO) 40 m radio telescope has observed 4C +21.35 at 15 GHz regularly since the end of 2007 (Richards et al. 2011). This monitoring program includes about 1700 known or likely γ-ray-loud blazars, including all candidate γ-ray blazar survey (CGRaBS) sources above declination −20°. The sources in this program are observed in total intensity twice per week with a 4 mJy (minimum) and 3% (typical) uncertainty on the flux density. Observations are performed with a dual-beam (each 2.5 arcmin full-width half-maximum) Dicke-switched system using cold sky in the off-source beam as the reference. Additionally, the source is switched between beams to reduce atmospheric variations. The absolute flux density scale is calibrated using observations of 3C 286, adopting the flux density (3.44 Jy) from Baars et al. (1977). This results in about a 5% absolute scale uncertainty, which is not reflected in the plotted errors. 4C +21.35 was variable at 15 GHz during the OVRO monitoring (Figure 2), with a flux density ranging from 1.01 Jy (at MJD 55094) to 2.13 Jy (at MJD 55423).

6.5. UMRAO Data

UMRAO centimeter band total flux density observations were obtained with the University of Michigan 26 m paraboloid located in Dexter, Michigan, USA. The instrument is equipped with transistor-based radiometers operating at frequencies centered at 4.8, 8.0, and 14.5 GHz with bandwidths of 0.68, 0.79, and 1.68 GHz, respectively. Dual horn feed systems are used at 8 and 14.5 GHz, while at 4.8 GHz a single-horn, mode-switching receiver is employed. Each observation consisted of a series of 8–16 individual measurements over approximately a 25–45 minute time period, utilizing an on–off observing technique at 4.8 GHz, and an on–on technique (switching the target between the two feed horns, which are closely spaced on the sky) at 8.0 and 14.5 GHz. As part of the observing procedure, drift scans were made across strong sources to verify the telescope pointing correction curves, and observations of nearby calibrators (3C 274, 3C 286, and 3C 218) were obtained every 1–2 hr to correct for temporal changes in the antenna aperture efficiency.

6.6. Medicina Data

We observed 4C +21.35 with the Medicina radio telescope five times between 2010 April 26 and 2010 May 11. We used the new Enhanced Single-dish Control System (ESCS) acquisition system, which provides enhanced sensitivity and supports observations with the cross scan technique. We observed at 22 GHz in the first four epochs, and at 5 GHz in the last two; the observations on 2010 May 10 were carried out at both frequencies and can be used for an estimate of the simultaneous spectral index. At each epoch, the source was observed for about 10 minutes and calibrated with respect to 3C 286, after correcting the data for atmospheric opacity. The observing conditions varied from epoch to epoch, resulting in different noise levels and significance of the detections. However, after flagging bad scans, we always obtained a highly significant ($\geq 5\sigma$) detection. The relative uncertainty on the estimated flux density at 22 GHz varies between 4% and 15%, while at 5 GHz it is around 3%.

6.7. MOJAVE Data

4C +21.35 is part of the Monitoring of Jets in Active Galactic Nuclei with VLBA Experiments (MOJAVE) sample, allowing us to investigate at 15 GHz the radio structure and jet kinematics of this source over a long period. The data were processed using the standard procedures described in the AIPS cookbook99 (for details, see Lister et al. 2009). The radio properties of 4C +21.35 strongly indicate that it has a relativistic jet beamed very closely along our line of sight. The kiloparsec scale radio morphology from Very Large Array images (Cooper et al. 2007; Saikia et al. 1993) consists of a bright jet starting out to the northeast of a bright core, and gradually curving to the east, terminating in a hotspot located approximately 60 kpc from the core. Surrounding the core is a circular halo of diffuse radio emission ~100 kpc in diameter, which is consistent with a large radio lobe being viewed end-on. On parsec scales, 4C +21.35 displays a compact radio jet at an initial position angle of ~0° that curves roughly 7° to the east over 10 mas. However, there is also a more distant feature at position angle ~6° from the optically thick core. Multi-epoch Very Long Baseline Array (VLBA) observations by the MOJAVE survey, using data from 1996 until 2011 May (for details of the fitting method, see Lister et al. 2013) show that this outermost feature (id = 1) has an apparent superluminal motion of 8.4c, and is moving to the east (Figure 4). Several other jet features closer in have faster speeds, all close to 17c, and are also accelerating to the east. There are two components (ids = 6,7) with even faster speeds of 20c and 27c (Table 3), that have trajectories curving to the west. These kinematic observations suggest complex three dimensional trajectories, perhaps having a helical form, which are being investigated in further detail by the MOJAVE collaboration. The linear fractional polarization and electric vector direction of the core feature changed between 2009 December and 2010 July, but remained relatively constant from 2010 July to December (Figure 5). There is evidence for a new bright jet feature in the core region as of 2009 November. The electric vector directions of the moving features further down the jet were remarkably uniform with time, pointing in a direction roughly perpendicular to the motion vector of the outermost moving features. On the other hand, there was no evidence at 15 GHz of a bright superluminal knot ejection during the 2010 γ-ray flaring period.

7. DISCUSSION

7.1. Light Curves Behavior and Correlation

The multifrequency light curve of 4C +21.35 in Figure 6 shows the Fermi-LAT, Swift (XRT; UVOT, u and m2 filters), optical R band (Abastumani, ATOM, Crimea, KVA, St. Petersburg), and radio from 15 GHz to 37 GHz (Effelsberg, Medicina, Metsähovi, OVRO, UMRAO) data collected during 2010 April 9–August 4 (MJD 55295–55412). In addition the γ-ray and X-ray photon indices observed by Fermi-LAT and Swift-XRT are reported in the second and fourth panels. The Fermi-LAT light curve shows two distinct γ-ray flaring episodes, peaking on 2010 April 29 (MJD 55315) and June 18 (MJD 55365), together with other peaks of lesser brightness. The two major γ-ray peaks detected by Fermi-LAT occurred very close in time to the VHE detections by MAGIC, on May 3 and June 17. This indicates that the same emission mechanism may be responsible for both the HE and VHE emission during these flaring episodes, in agreement also with the fact that the combined HE and VHE spectrum in 2010 June 17, corrected for the EBL absorption, can be described by a single power-law

99 http://www.aips.nrao.edu
Figure 4. Plot of angular separation from core vs. epoch for fitted Gaussian jet components in 4C +21.35. Color symbols indicate robust components for which kinematic fits were obtained (dotted and solid lines). The solid lines indicate vector motion fits to the data points assuming no acceleration, while the dotted lines indicate accelerated motion fits. Thick lines are used for components whose fitted motion is along a radial direction from the core, while the thin lines indicate non-radial motions. Unfilled black circles indicate non-robust components. The component identification numbers are located next to the last epoch of each robust component.

(A color version of this figure is available in the online journal.)

Figure 5. Total intensity and linear polarization images of 4C +21.35 observed by VLBA at 15 GHz in different epochs as part of the MOJAVE program. Naturally weighted total intensity images are shown by black contours, the contours are in successive powers of two times the base contour level of 0.2 mJy beam$^{-1}$. Electric polarization vectors direction is indicated by blue sticks, their length is proportional to the polarized intensity.

(A color version of this figure is available in the online journal.)

(Aleksić et al. 2011). It is also worth noting that during the two VHE detections the photon index estimated in the LAT energy range is quite flat ($\Gamma_{\gamma} \sim 2$), favoring the detection of $\gamma$-ray emission up to hundreds of GeV.

During 2010 February–June, Swift/XRT observed 4C +21.35 with a 0.3–10 keV flux in the range ($2.6$–$7.7$) $\times 10^{-12}$ erg cm$^{-2}$ s$^{-1}$, with the photon index changing in the range 1.4–2.2. The photon index remained constant during the 2010 April and June $\gamma$-ray flaring periods (see Figure 6). The very small variability amplitude observed in X-rays ($\sim 3$) with respect to the MeV–GeV energy range ($\sim 70$) could indicate that the low-energy segment of the electron energy distribution responsible for the production of the X-ray photons varies much less than the high-energy electron tail involved in the production of the observed $\gamma$-ray emission. A small variability amplitude was observed in UV during 2010. This could be due to the fact that the UV part of the spectrum is dominated by the accretion disk emission that dilutes the jet emission. It is worth noting that a peak of the UV emission was detected on June 18, but the small increase observed makes it unlikely that the change of the accretion rate is the main driver of the simultaneous activity observed at the higher energies by MAGIC and Fermi-LAT.

The $R$-band light curve is quite well sampled and shows variable flux density over time, but no dramatic increase of the activity. Two optical peaks were observed on 2010 April 20 (MJD 55306) and 2010 June 30 (MJD 55377), close in time but not simultaneous with the two $\gamma$-ray peaks. For the second flaring event, the lack of strictly simultaneous ground-based optical observations was covered by the UVOT observations that seems to indicate a relatively high activity at MJD 55367 (June 20). Correlations between the $\gamma$-ray and optical light curves of 4C +21.35 were investigated by computing the discrete cross correlation function (DCCF), following Edelson and Krolik (1988) and White and Peterson (1994; see Figure 7; positive lag means that $\gamma$-ray flux variations occur before those in $R$ band; the DCCF value ranges from $-1$ to $+1$). Although the overall $R$-band flux was higher during the period of $\gamma$-ray activity (see Figure 8) the DCCF shows no clear evidence for correlations on the timescale of the rapid flares ($\sim$days), with a maximum correlation of 0.4 for a time-lag of $\sim$35 days. A similar conclusion was reached by Smith et al. (2011) from a comparison of a LAT light curve during this epoch with the Steward Observatory $V$-band observations also used in this paper. In particular, overall correlation between the $\gamma$-ray band with the $R$ band was observed for 4C 21+35 during the 2010 $\gamma$-ray flaring activity, but on short time scales some differences
Table 3
Kinematic Fit Properties of Jet Components

<table>
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<tr>
<th>I.D.</th>
<th>N</th>
<th>(S) (mJy)</th>
<th>(R) (mas)</th>
<th>(θ) (deg)</th>
<th>⟨φ⟩ (deg)</th>
<th></th>
<th>⟨φ⟩ − φ⟩ (deg)</th>
<th>μ (μas yr⁻¹)</th>
<th>βapp (c)</th>
<th>μ⊥ (μas yr⁻²)</th>
<th>μ∥ (μas yr⁻²)</th>
<th>Tej (yr)</th>
<th>Tmid (yr)</th>
<th>Δα (μas)</th>
<th>Δδ (μas)</th>
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<td>1</td>
<td>24</td>
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<td>13.5</td>
<td>354.1</td>
<td>11.5 ± 1.4</td>
<td>17.4 ± 1.4^b</td>
<td>320.4 ± 9.3</td>
<td>8.41 ± 0.24</td>
<td>0.049 ± 0.017</td>
<td>−0.038 ± 0.021</td>
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<td>245</td>
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<td>20</td>
<td>7.4</td>
<td>7.4</td>
<td>15.7 ± 1.2</td>
<td>8.2 ± 1.2^b</td>
<td>581 ± 17^a</td>
<td>15.26 ± 0.43</td>
<td>0.092 ± 0.019</td>
<td>−0.007 ± 0.026</td>
<td>2002.49</td>
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<td>3.7</td>
<td>2.7</td>
<td>10.19 ± 0.27</td>
<td>7.48 ± 0.30^b</td>
<td>640.6 ± 8.4^a</td>
<td>16.82 ± 0.22</td>
<td>0.0730 ± 0.0055</td>
<td>0.005 ± 0.015</td>
<td>2000.88</td>
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<td>4.3</td>
<td>9.71 ± 0.39</td>
<td>5.41 ± 0.46^b</td>
<td>638.9 ± 5.1^a</td>
<td>16.77 ± 0.13</td>
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<td>6.2 ± 1.1</td>
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<td>1013 ± 39^a</td>
<td>26.6 ± 1.0</td>
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<td>8</td>
<td>2.1</td>
<td>0.9</td>
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<td>0.71 ± 0.92</td>
<td>632 ± 45</td>
<td>16.6 ± 1.2</td>
<td>0.012 ± 0.038</td>
<td>0.23 ± 0.15</td>
<td>2006.55 ± 0.25</td>
<td>2009.26</td>
<td>36</td>
<td>168</td>
<td></td>
</tr>
<tr>
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<td>4.3</td>
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<td>444 ± 35</td>
<td>11.67 ± 0.92</td>
<td>...</td>
<td>...</td>
<td>2007.82 ± 0.20</td>
<td>2009.93</td>
<td>49</td>
<td>87</td>
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</tr>
<tr>
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<td>9</td>
<td>27</td>
<td>7.5</td>
<td>5.2</td>
<td>357.8 ± 1.7</td>
<td>19.9 ± 2.3^b</td>
<td>615 ± 23</td>
<td>16.15 ± 0.60</td>
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<td>...</td>
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<td>...</td>
<td>2010.55</td>
<td>6</td>
<td>26</td>
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</tbody>
</table>

Notes. The kinematic fit values are derived from the acceleration fit for components with significant acceleration, and from the vector motion fit otherwise. Columns are as follows: (1) component number, (2) number of fitted epochs, (3) mean flux density at 15 GHz in mJy, (4) mean distance from core component in mas, (5) mean position angle with respect to the core component in degrees, (6) position angle of velocity vector in degrees, (7) offset between mean position angle and velocity vector position angle in degrees, (8) angular proper motion in microarcseconds per year, (9) fitted speed in units of the speed of light, (10) angular acceleration perpendicular to velocity direction in microarcseconds per year per year, (11) angular acceleration parallel to velocity direction in microarcseconds per year per year, (12) fitted ejection date, (13) date of reference (middle) epoch used for fit, (14) right ascension error of individual epoch positions in μas, (15) declination error of individual epoch positions in μas.

^a Component shows significant accelerated motion.
^b Component shows significant non-radial motion.
Figure 6. Multifrequency light curves of 4C +21.35 between 2010 April 9 and August 4 (MJD 55295–55412). The data sets were collected (from top to bottom) by Fermi-LAT \((E > 100 \text{ MeV})\); in units of \(10^{-6} \text{ photons cm}^{-2} \text{ s}^{-1}\); taken from Tanaka et al. 2011), Swift-XRT (0.3–10 keV; in units of \(10^{-12} \text{ erg cm}^{-2} \text{ s}^{-1}\)), Swift-UVOT (m2 filter; in units of mJy), Swift-UVOT (U filter, open circles; in units of mJy), Abastumani, ATOM, Crimean, St. Petersburg (R-band, filled triangles; in units of mJy), Effelsberg, Medicina, Metsähovi, OVRO, UMRAO (15 GHz: filled circles, 23 GHz: open squares, 37 GHz: open triangles; in units of Jy). The downward arrows indicate the times of the VHE detections by MAGIC. For clarity the \(m_2\), \(u\), \(R\) and 15 GHz bands errors (typically 5% or less) and the \(\gamma\)-rays errors are not shown.

Figure 7. Discrete cross correlation function between the \(\gamma\)-ray and \(R\)-band light curves of 4C +21.35. It is evident (see Figure 8). A complex connection between the optical and \(\gamma\)-ray emission has been already observed in several FSRQs and low-synchrotron-peaked BL Lacertae objects. In some cases a clear optical/\(\gamma\) correlation with no lags was observed (e.g., 3C 279; Abdo et al. 2010). But sometimes no correlation was found between these two energy bands (e.g., BL Lac; Abdo et al. 2011), and in other occasions, an optical and NIR flare with no significant counterpart in \(\gamma\)-rays was observed (e.g., PKS 0208−512 and PKS 0537−441; Chatterjee et al. 2013; D’Ammando et al. 2013).

An increasing flux density was observed in radio and mm bands from the beginning of 2009 (see Figure 2) contemporaneous with the increasing \(\gamma\)-ray activity observed by Fermi-LAT, reaching the peak of the flux density at 230 GHz on 2011 January 27 (MJD 55588). Interestingly, the peak of the 23 GHz and 37 GHz was observed on 2010 May 10 (MJD 55326) and June 18 (MJD 55365), respectively, close in time with the major \(\gamma\)-ray flares. The same activity was also observed at 8 GHz and 5 GHz, with the emission peak delayed likely due to synchrotron self-absorption opacity effects. However, the sparse coverage does not allow us to obtain conclusive evidence. A significant spectral evolution was also observed in radio (see Figure 3), with the spectrum changed from steep on 2009 January 24 (\(\alpha_r = 0.3\)) to inverted (\(\alpha_r = -0.2\)) on 2011 April 29 (see Section 6.2).

7.2. SED Modeling

7.2.1. Data Selection

We have built three quasi-simultaneous SEDs from the data discussed above, shown in Figure 9. These SEDs include the flaring states of 2010 June 17 (red circles) and 2010 April 29 (green squares), and a quiescent state, integrated in time from 2008 August 4 to 2008 September 12 (blue diamonds). For the three SEDs we used the LAT spectra calculated over 2010 June 17, 2010 April 23–May 2, 2008 August 4–2009 September 12 (taken from Tanaka et al. 2011; Aleksić et al. 2011), and the Swift data collected on 2010 June 20, 2010 April 23, and 2009 April 10, respectively. The MAGIC data collected on 2010 May 3 and June 17 are included for the two flaring states. These data have been corrected for EBL absorption using the model of Finke et al. (2010). This model is
nearly identical in the energy range covered by MAGIC to the model of Dominguez et al. (2011) used in Aleksić et al. (2011). We also included the radio and R-band observations nearest to the LAT $\gamma$-ray peak for the two flaring states (2010 April 28 and June 22, respectively), and the Swift observation performed on 2009 April 19 for the quiescent state. Finally we report in the SEDs the average Swift BAT 70 month spectrum, the Planck spectrum collected in 2009 December (Ade et al. 2013), and the Spitzer data from Malmrose et al. (2011)

Farina et al. (2012) estimate the black hole (BH) mass for 4C +21.35 as $M_{\text{BH}} \sim 6 \times 10^8 M_\odot$, using broad emission line measurements from over 100 optical spectra from a variety of sources. This value agrees with values found by Shen et al. (2011) and Shaw et al. (2012) with an Sloan Digital Sky Survey (SDSS) spectrum, but significantly greater than the value found by Wang et al. (2004) and used by Tanaka et al. (2011), $M_{\text{BH}} \sim 1.5 \times 10^9 M_\odot$. It is worth noting that the measurement by Wang et al. (2004) relies on the H-$\beta$ broad line and the continuum luminosity-BLR radius relation from Kaspi et al. (2000). That relation was obtained from reverberation mapping of a small number of active galactic nuclei using a cosmology with a decelerating universe, which is now known to be incorrect. We use the more precise value from Farina et al. (2012) in our SED modeling.

7.2.2. Model

We model the SED of the three epochs using a one-zone leptonic model. We began our modeling efforts by attempting to model the IR data from Malmrose et al. (2011) with a blackbody dust torus. The results for the luminosity ($L_{\text{dust}}$) and temperature ($T_{\text{dust}}$) of the blackbody were similar to the ones found by Malmrose et al. (2011). The optical emission clearly appears to be dominated by thermal disk emission, rather than nonthermal synchrotron emission from the jet, otherwise the optical spectrum would appear much softer. Therefore, we next modeled the optical data in the low-state with a Shakura–Sunyaev multi-temperature disk (Shakura & Sunyaev 1973), assuming $M_{\text{BH}} \sim 6 \times 10^8 M_\odot$. We note that the disk fit to the low-state data is insensitive to the inner radius of the disk, $R_{\text{in}}$, as seen in a close up of this part of the SED in Figure 10. Parameters for the dust torus, accretion disk, and all other modeling parameters can be found in Table 4. Tavecchio et al. (2011) use an isotropically emitting blackbody spectrum to fit the blue bump and obtain a value for the disk luminosity over twice the value presented here. We use a Shakura–Sunyaev disk, which does not emit isotropically, and which we assume emits as the cosine of the disk inclination angle. With this distribution, for a face-on disk, the flux will be twice that from an isotropic distribution for a given luminosity (e.g., Castignani et al. 2013). This is the cause of most of the discrepancy, with the remaining discrepancy due to the different contributions from nonthermal synchrotron emission.

Although several possibilities have been suggested for the origin of $\gamma$-ray emission from 4C+21.35 (see Section 1), FSRQ-type blazars such as 4C +21.35 are expected to have their $\gamma$-rays originate from the external Compton (EC), rather than synchrotron self-Compton (SSC) mechanism (e.g., Ghisellini et al. 1998). Therefore we next attempt to fit the SED in the high state of 2010 June 17 (MJD 55364) with a combination of synchrotron, SSC, and EC emission from a jet blob moving at a highly relativistic speed. We assume an emitting size of $R'_e = 10^{15}$ cm in the comoving frame, consistent with the rapid variability timescale of 10 minutes. The dust torus and disk emission are not varied between flaring and quiescent states. For the nonthermal jet emission we choose a variability timescale of 10 minutes, consistent with the variability observed by MAGIC (Aleksić et al. 2011). The MAGIC detection of the source out to $\gtrsim 300$ GeV also implies the primary emitting region must be outside the BLR, otherwise $\gamma\gamma$ absorption by broad-line photons would not allow such high-energy $\gamma$-ray photons to escape (Tanaka et al. 2011; Aleksić et al. 2011), so we chose a large jet distance from the BH, $r$, outside the BLR radius of $R_{\text{BLR}} \approx 2 \times 10^{17}$ cm (Tanaka et al. 2011). Outside the BLR, the seed photon source is expected to be from the dust torus, which is what we use as the EC seed photon source. For the purposes of calculating the geometry of Compton scattering,
we assume the dust torus is a one-dimensional ring with radius $R_{\text{dust}}$, aligned orthogonal to the jet, where we choose $R_{\text{dust}}$ to be roughly consistent with the value of the dust sublimation radius calculated by Nenkova et al. (2008). This is necessary since our calculations use the full angle-dependent Compton cross section, accurate in the Thomson through Klein-Nishina (KN) regimes. The adopted synchrotron component is self-absorbed below $10^{12}$ Hz. We treat the radio points as upper limits, since their slow variability compared to the optical and flat spectrum (in flux density (Konigl 1981), and not the result of the same emitting region implies they are probably the result of a superposition of several self-absorbed jet components (Konigl 1981), and not the result of the same emitting region that produces the rest of the SED. The electron distribution was assumed to be a broken power law between electron Lorentz factors $\gamma_{\text{min}}$ and $\gamma_{\text{max}}$, with power-law index $p_1$ for $\gamma < \gamma_{\text{min}}$ and $p_2$ for $\gamma > \gamma_{\text{max}}$. Further details on the model and its parameters can be found in Finke et al. (2008) and Dermer et al. (2009).

The result of this fit to the 2010 June 17 (MJD 55364) SED is shown in Figure 9. We note that there is some degeneracy in the choice of the model parameters, hence the set of parameter values describing the observational data are not unique. However, we do demonstrate that a one-zone model can adequately describe the data. To account for the highest speeds derived by the jet kinematics analysis of the MOJAVE data (see Section 6.7) at least some portion of the jet must be viewed within $\sim 4^\circ$ of the line of sight. To avoid the extreme KN regime for Compton scattering, we found that the jet needs to be highly aligned, with the jet angle with respect to the line of sight $\theta \sim 0^\circ$ ($\delta_D \sim 21^\circ$), where $\delta_D$ is the Doppler factor. This is because the energy at which the extreme KN regime begins is at $E_{\text{KN}} \approx (\delta_D/T)\epsilon_0$, where $\epsilon_0$ is the seed photon energy. Such a small jet’s angle does not disagree with the high apparent speeds estimated on the scales of a few parsecs if the complex three dimensional trajectories observed by MOJAVE are taken into consideration. In fact, there is evidence for a bend in the jet on the parsec scale in the VLBA images, where the emission in this model originates (see Section 6.7). The model does not provide a good fit to the XRT data in this SED, with the model being dominated by synchrotron emission for the soft X-rays, while the XRT spectral index is $\Gamma_X < 2$ indicating it is dominated by some sort of Compton scattering, either SSC or EC (EC in the case of our model fit). However, the XRT data were not strictly simultaneous with the rest of the SED, particularly the LAT data (with a gap of six and three days between the X-ray and $\gamma$-ray data, respectively. As can be seen in Figure 6, the XRT photon index alternates between $\Gamma_X < 2$, implying Compton scattering dominates in this waveband, and $\Gamma_X > 2$, implying synchrotron dominates. If the primary emitting region makes up the majority of the jet cross section, this model fit gives a jet half-opening angle of $\theta_{\text{open}} \sim R_{\text{jet}}/r \sim 10^{-4}$ rad $\sim 0.007$, where $R_{\text{jet}}$ is the comoving radius of the blob. Such a small opening angle is highly unlikely and inconsistent with radio observations (Figure 5), so this model implies that the overwhelming majority of the source’s emission is coming from a very small fraction of the jet’s cross section. We also calculated the jet power in electrons ($P_{\text{j},e}$) and Poynting flux ($P_{\text{j},B}$) for this model fit, assuming a two-sided jet (Finke et al. 2008), finding that the source has almost 100 times as much power in electrons as in Poynting flux. The model fit to the 2010 June 17 (MJD 55364) flaring SED is similar to the “case A” fit to the same SED data by Tavecchio et al. (2011). They also found a jet where the electron energy density dominates over the magnetic energy density, although in their case it is even more dominant, with $P_{\text{j},e} \sim 10^8 P_{\text{j},B}$. Tavecchio et al. (2011) also provide two other fits to the same SED with two zone models; a “case B” where there is an additional contribution from a larger blob outside the BLR; and a “case C” where there is a contribution from a larger blob inside the BLR. Neither of these two-zone fits solves the problem of having an extremely small, bright blob at a large distance from the BH, although they do provide fits much closer to equipartition between electrons and Poynting flux. The UV data for the 2010 June 17 flaring SED requires an inner disk
Indeed, our fits favor stable circular orbit around a nonrotating Schwarzschild BH. This is because, as seen in the figure, a larger radius will not fit the UV data. The results depend on the BH mass, although for this to seem to converge to around $6 \times 10^9 M_\odot$, we also note that if the BH mass were as low as the one found by Wang et al. (2004), $M_{\text{BH}} = 1.5 \times 10^8 M_\odot$, we would not be able to fit the blue bump for this source with a value of the disk luminosity $L_{}\text{disk}$ that is less than the Eddington luminosity. The UV data are often subject to heavy extinction, which could lead to large uncertainty. If the synchrotron component was less steep it could also potentially have a greater contribution to the UV region, masking a larger $R_g$. But in this case the synchrotron emission would over-predict the longer wavelength optical data, so this is unlikely. Finally, the disk model we use is rather simple. It does not include a general relativistic effects such as gravitational Doppler shifts or light bending (Li et al. 2005).

For the model in this scenario, $L_{\text{iso}} = L_{\text{BLR}}/\xi_{\text{disk}}$ is the source luminosity and $L_{\text{iso}} = 10^{45}$ erg s$^{-1}$ (Fan et al. 2005) found a tight correlation between $L_{\text{iso}}$ and $L_{\text{BLR}}$, and all the values here, which are around $L_{\text{iso}} = 5 \times 10^{45}$ erg s$^{-1}$. Greene & Ho (2005) found a tight correlation between $L_{\text{iso}}$ and $L_{\text{BLR}}$, and all the values here, which are around $L_{\text{iso}} = 5 \times 10^{45}$ erg s$^{-1}$, are consistent with their correlation. If the total BLR luminosity $L_{\text{BLR}} = 25.3 \times L_{\text{iso}}$ (Tanaka et al. 2011), then, using a value $L_{\text{iso}} = 5 \times 10^{45}$ erg s$^{-1}$ that is consistent with the recent measurements (Shen et al. 2011; Shaw et al. 2012; Farina et al. 2012) one gets $L_{\text{iso}} = 3.5 \times 10^{45}$ erg s$^{-1}$. Thus, using the disk luminosity for our model, one gets $\xi_{\text{disk}} = L_{\text{iso}}/L_{\text{BLR}} \approx 0.08$, a fairly standard value. Our model fits give a value of the fraction of the disk radiation reprocessed in the dust torus $\xi_{\text{disk}} = 0.34$, again a fairly standard value (e.g., Sikora et al. 2009).

### 7.2.3. Accretion Disk Emission

For both the flaring state models, we find that a good fit to the UV data from Swift-UVOT requires an inner disk radius $R_{\text{in}} < 6R_g$, where $6R_g$ is the value one would expect for the innermost stable circular orbit around a nonrotating Schwarzschild BH. Indeed, our fits favor $R_{\text{in}} = 3R_g$ (see Figure 10), the value one would expect for a maximally (prograde) rotating Kerr BH. This is because, as seen in the figure, a larger $R_{\text{in}}$ will not fit the UV data points. We also performed fits with the color correction of Chiang (2002). This requires a slightly higher disk luminosity ($L_{\text{disk}} = 2 \times 10^{46}$ erg s$^{-1}$), but our results for the inner disk radius remain unchanged. This is of interest since one would expect a BH spin at or near the maximum value if the jet is generated from the Blandford–Znajek mechanism (Blandford & Znajek 1977). It is also inconsistent with the scenario of Garofalo et al. (2010), where the jets in powerful FR II sources (and presumably FSRQs) are produced by BHs with retrograde spin, requiring that $R_{\text{in}} > 6R_g$, while jets in less powerful FR I sources (and presumably BL Lac objects) are produced by BHs with prograde spin. However, there are some caveats regarding the fit of the optical/UV data. The results depend on the BH mass, although for this to seem to converge to around $6 \times 8 \times 10^9 M_\odot$. We also note that if the BH mass were as low as the one found by Wang et al. (2004), $M_{\text{BH}} = 1.5 \times 10^8 M_\odot$, we would not be able to fit the blue bump for this source with a value of the disk luminosity $L_{\text{disk}}$ that is less than the Eddington luminosity. The UV data are often subject to heavy extinction, which could lead to large uncertainty. If the synchrotron component was less steep it could also potentially have a greater contribution to the UV region, masking a larger $R_g$. But in this case the synchrotron emission would over-predict the longer wavelength optical data, so this is unlikely. Finally, the disk model we use is rather simple. It does not include a general relativistic effects such as gravitational Doppler shifts or light bending (Li et al. 2005).

### 7.2.4. Jet and Accretion Power

Our model fits give a total accretion power of $P_{\text{acc}} = L_{\text{iso}}/\eta_{\text{disk}} = 1.9 \times 10^{47}$ erg s$^{-1}$. If the bolometric isotropic equivalent luminosity from the 2010 June 17 flare is $L_{\text{iso}} = 10^{45}$ erg s$^{-1}$ (Tanaka et al. 2011) then the radiative efficiency of the flare is $\eta_j \approx 0.7$.

(Finke et al. 2008; Sikora et al. 2009; Tanaka et al. 2011, where the factor of 2 takes into account the two-sided jet), which implies a highly radiatively efficient jet. The estimate for the total jet power, $P_j = P_j,e + P_j,B + P_{j,p}$, is a lower limit because it does not include a contribution from protons in the jet ($P_{j,p}$), which are likely to be present (e.g., Sikora & Madejski 2000; Sikora et al. 2009). The jet power contributes a fraction of the total accretion power of

$$\frac{P_j,e + P_j,B}{P_{\text{acc}}} = 2.3 \times 10^{-3}.$$
although again note that this is a lower limit due to the uncertainty of the proton content. In fact, requiring that $P_j / P_{\text{acc}} < 1$ gives a constraint on the power in the jets $P_{j,p} \lesssim 440 P_{j,e}$. A low $P_j / P_{\text{acc}}$ is at odds with the conclusions of Tanaka et al. (2011) who estimate a much higher $P_j / P_{\text{acc}}$. The difference is due to their assuming a smaller $\Gamma$ and $\eta_j$ than our derived values.

It is interesting to explore the possibility that the flare occurs inside the BLR, and the break in the LAT spectrum is due to $\gamma\gamma$ absorption of $\gamma$-rays with He $\text{ii}$ Ly photons (continuum and lines) (Poutanen & Stern 2010; Stern & Poutanen 2011). Following Tanaka et al. (2011), we find that

$$L_{\text{He} \text{ii} \gamma} \simeq 0.1 L_{\text{He} \text{ii} \text{Ly}} \simeq 4.5 L_{\text{H}\beta} \simeq 2.2 \times 10^{44} \text{ erg s}^{-1},$$

where we have used the value for $L_{\text{H}\beta}$ discussed above. Assuming the typical radius for the He $\text{ii}$ emission is at a radius $R_{\text{He} \text{ii}} \simeq 0.5 R_{\text{BLR}}$, i.e., at $10^{17}$ cm, we find that the spectral break one expects from $\gamma\gamma$ absorption with He $\text{ii}$ Ly photons is

$$\Delta \Gamma \sim \frac{\tau_\gamma(5 \text{ GeV})}{4} \approx \frac{\sigma_{\text{e}} L_{\text{He} \text{ii} \gamma}}{16 \pi c E_{\text{He} \text{ii} \gamma} R_{\text{He} \text{ii}}} \simeq 1.2,$$

significantly larger than the $\Delta \Gamma \simeq 0.5$ found in the LAT spectrum for 4C +21.35. The uncertainty in broad emission line luminosities seems to make this approximation a rough estimate. We note that a disk wind model for the BLR (Murray et al. 1995; Chiang & Murray 1996; Murray & Chiang 1996) would lower the $\gamma\gamma$ opacity of the BLR, relative to a spherical shell geometry. We tested this possibility, however, and found that the $\gamma\gamma$ opacity remains extremely high, so it is still highly unlikely that MAGIC-detected $\gamma$-ray photons could escape the BLR.

8. CONCLUSIONS

4C +21.35 was detected at VHE by MAGIC on 2010 June 17 during a period of high $\gamma$-ray activity detected by Fermi-LAT. The relatively hard spectrum of the combined HE and VHE spectrum ($\Gamma = 2.7 \pm 0.3$), with no evidence of a cutoff, together with the very rapid variability ($\sim 10$ minutes) observed by MAGIC challenge standard emission models. We presented multifrequency observations of the FSRQ 4C +21.35 collected from radio to VHE during 2009–2010. The first hint of a signal at VHE by MAGIC was found on May 3, during a further period of $\gamma$-ray activity observed by Fermi, suggesting a common origin for both the HE and VHE emission during the 2010 April and June episodes.

During 2010 February–June only moderate flux variability was observed in X-rays (a factor of $\sim$three), with the photon index changing in the range 1.4–2.2 but with no correlation between flux and photon index. A low variability amplitude was observed in UV in the same period, suggesting that the UV is dominated by the accretion disk emission that dilutes the jet emission. It is worth noting that the peak of the UV emission was detected on June 18, but the small increase observed makes it unlikely that the change of the accretion rate is the main driver of the HE and VHE high activity detected by Fermi and MAGIC. The optical light curve shows variable flux density, but no dramatic increase of the activity. Two optical peaks were observed on 2010 April 20 (MJD 55306) and 2010 June 30 (MJD 55377), close in time but not simultaneous with the $\gamma$-ray peaks.

Based on the 15 GHz MOJAVE data, there is no evidence for the ejection of super-luminal knots associated with either of the flares in 2010 April and June. However, Marscher et al. (2012) detected the ejection of a superluminal knot with 43 GHz imaging at a time somewhere between 2010 April 29 and June 3 (MJD 55315–55350), close in time with the first 2010 $\gamma$-ray flare (see their Figure 3). We also noted that this knot could be associated with the $\gamma$-ray outburst at around 2010 May 24 (MJD 55340). If the flare occurred at the 43 GHz core, our model implies that the 43 GHz core is about 3 pc from the central BH.

Based on our SED modeling (Section 7.2), we reach the following conclusions.

1. The $\gamma$-ray flares in 2010 April and June cannot have originated from inside the BLR, at least not without invoking some unusual particle transport mechanism (Dermer et al. 2012; Tavecchio et al. 2012).
2. There is some evidence for a rapidly spinning prograde BH based on the optical emission.
3. The two flaring states and the quiescent state can be modeled by varying only the electron distribution for the source.

The last result, modeling the source by varying only the electron distribution, has also been found for the blazar PKS 0537–441 (D’Ammando et al. 2013). This conclusion is much stronger for PKS 0537–441, since the optical continuum of PKS 0537–441 is not disk-dominated, making its modeling more constraining. Nonetheless, there are clearly sources for which a change in the electron distribution is not sufficient to explain the difference between flaring and quiescent states. For example, to model a strong optical-near infrared flare from PKS 0208–512 with no counterpart in $\gamma$-rays required changing the magnetic field strength (Chatterjee et al. 2013).

Rotation in polarization angles coincident with flares has been observed before in the blazars BL Lac (Marscher et al. 2008), PKS 1510–089 (Marscher et al. 2010; Orienti et al. 2013), and 3C 279 (Abdo et al. 2010). They could be caused by a sudden realignment in the magnetic field due to shock compression, or a curved trajectory taken by the flaring region. A slight increase of the degree of optical polarization but no significant rotation of the polarization angle was observed at the time of the 2010 June HE and VHE flare.

The object 4C +21.35 continues to challenge our understanding of blazar emission mechanisms and the location of the emitting region. Multi-wavelength observations have complemented previous LAT and MAGIC observations to give a more complete picture for this source, although many outstanding questions remain.

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