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Foreshock Properties at Typical and Enhanced Interplanetary Magnetic Field Strengths: Results From Hybrid-Vlasov Simulations

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Abstract In this paper, we present a detailed study of the effects of the interplanetary magnetic field (IMF) strength on the foreshock properties at small and large scales. Two simulation runs performed with the hybrid-Vlasov code Vlasiator with identical setup but with different IMF strengths, namely, 5 and 10 nT, are compared. We find that the bow shock position and shape are roughly identical in both runs, due to the quasi-radial IMF orientation, in agreement with previous magnetohydrodynamics simulations and theory. Foreshock waves develop in a broader region in the higher IMF strength run, which we attribute to the larger growth rate of the waves. The velocity of field-aligned beams remains essentially the same, but their density is generally lower when the IMF strength increases, due to the lower Mach number. Also, we identify in the regular IMF strength run ridges of suprathermal ions which disappear at higher IMF strength. These structures may be a new signature of the foreshock compressional boundary. The foreshock wave field is structured over smaller scales in higher IMF conditions, due to both the period of the foreshock waves and the transverse extent of the wave fronts being smaller. While the foreshock is mostly permeated by monochromatic waves at typical IMF strength, we find that magnetosonic waves at different frequencies coexist in the other run. They are generated by multiple beams of suprathermal ions, while only a single beam is observed at typical IMF strength. The consequences of these differences for solar wind-magnetosphere coupling are discussed.

Plain Language Summary Our solar system is filled with a stream of particles escaping from the Sun, called the solar wind. The Earth is shielded from these particles by its magnetic field, which creates a magnetic bubble around our planet, the magnetosphere. Because the solar wind flow is supersonic, a bow shock forms in front of the magnetosphere to slow it down. The outermost region of the near-Earth space is called the foreshock. It is a very turbulent region, filled with particles reflected off the Earth’s bow shock, and with a variety of magnetic waves. These waves can be transmitted inside the magnetosphere and create disturbances in the magnetic field on the Earth’s surface. In this work, we use supercomputer simulations to study how the foreshock changes when the solar magnetic field, carried by the solar wind, intensifies. This happens in particular during solar storms, which create stormy space weather at Earth and can have adverse consequences on, for example, spacecraft electronics and power grids. We find that the foreshock properties are very different during these events compared to normal conditions and that these changes may have consequences in the regions closer to Earth.

1. Introduction

Shocks are ubiquitous in our universe, from planetary bow shocks to supernova remnants. One key parameter controlling the properties of a magnetized shock is its obliquity, quantified by the angle $\Theta_{bn}$ between its normal direction and the upstream magnetic field. The nature of the shock transition changes dramatically depending on whether the shock is quasi-perpendicular ($\Theta_{bn} > 45^\circ$) or quasi-parallel ($\Theta_{bn} < 45^\circ$). This stems from the fact that in the latter case particles reflected at the shock front can escape far upstream along the magnetic field lines. The upstream region magnetically connected to a shock, which is populated by particles reflected off the shock front, is called the foreshock. The interaction of the backstreaming population
with the incoming solar wind triggers plasma instabilities, resulting in the development of intense wave activity, in particular in the ultralow-frequency (ULF) range, from 1 mHz to 10 Hz. Spacecraft observations in the Earth’s ion foreshock have evidenced the presence of 1-Hz and 3-, 10-, and 30-s waves, as well as shocklets and discrete wave packets (e.g., Burgess, 1997; Eastwood et al., 2003; Eastwood, Lucek, et al., 2005; Greenstadt et al., 1995; Hobara et al., 2007; Hoppe et al., 1981; Wilson III, 2016, and references therein).

The 30-s waves have been extensively studied, particularly because of the long-standing question of their observed oblique propagation, while theory predicts that they should propagate preferentially parallel to the magnetic field (e.g., Eastwood, Balogh, et al., 2005a; Gary, 1991; Hsieh & Shue, 2013; Palmroth et al., 2015). They are found in conjunction with intermediate, gyrophase-bunched, or gyrotropic ion distributions (Eastwood, Balogh, et al., 2005b). The 30-s waves are quasi-monochromatic fast magnetosonic waves generated via the ion-ion beam right-hand instability (Gary, 1991). They are right-hand polarized in the plasma frame and propagate with the ion beam, but because they are advected back to the bow shock by the solar wind flow, they appear as left-handed in the spacecraft frame (Eastwood, Lucek, et al., 2005). Their wavelength parallel to the magnetic field is about 1 RE (Earth radius = 6,371 km; Archer et al., 2005; Hoppe & Russell, 1983). The transverse extent of the wave fronts is much larger, of the order of 8 to 18 RE (Archer et al., 2005). Despite being called 30-s waves, their period actually ranges between 10 and 55 s in the terrestrial foreshock (Eastwood, Balogh, et al., 2005b). They have also been detected at other planetary foreshocks, such as Mercury, Venus, and Jupiter, where their frequency is roughly proportional to the interplanetary magnetic field (IMF) strength, with $f \sim 0.0068$ (nT) (Hoppe & Russell, 1982). Subsequent studies have shown that the IMF cone angle $\theta_{Bn}$ between the IMF vector and the Sun-Earth line, is another factor controlling the wave period (Le & Russell, 1996; Takahashi et al., 1984).

The edge of the ion foreshock is defined as the limit beyond which no counterstreaming ion beams are observed. Because of the drift due to the solar wind motional electric field, this boundary is located earthward of the tangent field line and is inclined toward the bow shock. Inward of the foreshock edge, field-aligned beams are observed but no wave activity. This is due to the finite growth time of the instability, which has not yet had time to grow in this region as the beams have not interacted long enough with the solar wind (e.g., Blanco-Cano et al., 2009). The ULF foreshock boundary marks where ULF waves start to develop (Andrés et al., 2015; Eastwood, Lucek, et al., 2005). More recent simulations and observations have evidenced another boundary deeper in the foreshock, where ULF waves become significantly compressive, termed the foreshock compressional boundary (Omidi et al., 2009; Rojas-Castillo et al., 2013). The ULF foreshock is populated by intermediate, gyrotropic, and gyrophase-bunched ion distributions, which become more and more distorted and have broader pitch angle distributions when moving toward the central foreshock. Diffuse distributions are detected in the vicinity of the bow shock (see, for example, Fuselier, 1995; Kempf et al., 2015; Wilson III, 2016, for more details on the ion distributions in the foreshock). Overall, the density of suprathermal ions, independently of their velocity distribution function (VDF), decreases with increasing distance from the bow shock (Kis et al., 2004; Kempf et al., 2015). In the field-aligned beam region, the velocity of the backstreaming particles increases with increasing $\theta_{Bn}$. It is therefore maximum at the foreshock edge and decreases toward the central foreshock (Burgess et al., 2012; Kempf et al., 2015).

In addition to its substantial spatial variability, the foreshock varies also temporally, as its properties are intimately coupled with the changing solar wind conditions. The position of the quasi-parallel shock, and thus that of the foreshock, is directly controlled by the direction of the IMF (Francia et al., 2012; Turc et al., 2015). The position of the foreshock boundaries is also dictated by the upstream solar wind conditions, in particular, the IMF orientation and the solar wind velocity, and also the Alfvén Mach number ($M_A$) in the case of the foreshock compressional boundary (Andrés et al., 2015; Eastwood, Lucek, et al., 2005; Omidi et al., 2009). As mentioned above, the frequency of the ULF waves has been shown to depend on the IMF cone angle and strength (Le & Russell, 1996). A decrease in the solar wind density results in a lower ULF wave activity (Francia et al., 2012; Le et al., 2000; Regi et al., 2014), while changes in the plasma $\beta$ can affect the development of wave modes (Hobara et al., 2007; Le et al., 1992). Enhanced fluxes of energetic ions are observed at large solar wind speeds (see, e.g., Kudela et al., 2005; Trattner et al., 1994), suggesting that acceleration at the bow shock is more efficient under these conditions. Moreover, recent studies have shown that the 30-s waves in the magnetic field are accompanied by oscillations of the energetic ion fluxes when the solar wind velocity is above 400 km/s (Petrukovich et al., 2017).
However, each of these studies focuses on one specific foreshock feature, and we are still missing the global picture of the consequences of a change in a given solar wind parameter. Such a study requires global kinetic simulations, since the magnetohydrodynamic description does not capture the foreshock, which is inherently a kinetic structure. Spacecraft measurements offer only a limited view of the foreshock, and disentangling the temporal and spatial variations can be challenging, even more so in large statistical surveys. Numerical simulations offer the opportunity to isolate the effects of a given solar wind parameter, thus facilitating the interpretation of the results. The foreshock has been extensively studied using hybrid-particle-in-cell (PIC) simulations (e.g., Blanco-Cano et al., 2006, 2009; Karimabadi et al., 2014; Omidi et al., 2005, 2013). In the hybrid-PIC approach, ions are treated as macroparticles, while electrons are considered as a fluid. A large fraction of hybrid-PIC global studies are two-dimensional (2-D) in real space, but 3-D hybrid-PIC simulations of the foreshock have also been performed (e.g., Lin & Wang, 2005; Omidi et al., 2017). An alternative is to model ions as VDF, using the so-called hybrid-Vlasov formalism. This approach has been adopted in the Vlasiator code (http://www.helsinki.fi/en/researchgroups/vlasiator), which simulates the near-Earth space, including the foreshock, in its real physical scales (von Alfthan et al., 2014). Although being computationally heavy, the hybrid-Vlasov description has the advantage of providing noiseless ion VDFs. A number of studies utilizing this model have been already published and have shown a good agreement with previous numerical and observational works (Hoolijoki et al., 2016, 2017; Kempf et al., 2015; Palmroth et al., 2015, 2017; Pfau-Kempf et al., 2016).

In this paper, we will concentrate on the effects of the IMF strength. This parameter is likely to influence significantly the foreshock properties because it directly controls the bow shock strength, quantified by the upstream magnetosonic Mach number, which in turn affects particle reflection at the shock front. It can also impact wave activity, since the plasma $\beta$ is a function of the IMF magnitude. Using the Vlasiator simulation model, we will compare the foreshock properties at two different IMF magnitudes, at 5 nT, corresponding roughly to its typical value at Earth, and at 10 nT, which is comparable to the magnetic field strength during geoeffective solar wind transients such as interplanetary coronal mass ejections, magnetic clouds, and corotating interaction regions. The manuscript is organized as follows: the simulation model is described in section 2, and the comparison of the two runs is presented in detail in section 3. We summarize and discuss our results in section 4.

2. Description of the Model

Vlasiator is a hybrid-Vlasov simulation code targeted at global modeling of the terrestrial magnetosphere and its interaction with the solar wind while retaining ion kinetic physics (von Alfthan et al., 2014). In the hybrid-Vlasov approach, ions are described as VDFs, while electrons are considered as a massless charge-neutralizing fluid. The evolution of the system is obtained by solving the Vlasov equation, self-consistently coupled with Maxwell’s equations. Closure is provided by the generalized Ohm law, with the Hall term included. A detailed description of the model can be found in von Alfthan et al. (2014) and Pfau-Kempf (2016). The main advantage of the hybrid-Vlasov approach is that it does not rely on statistical sampling of the phase space, as is done in PIC simulations (e.g., Blanco-Cano et al., 2006; Karimabadi et al., 2014; Omidi et al., 2005), but provides a noiseless description of the ion VDFs. Also, the full geomagnetic dipole strength can be used in Vlasiator. Both temporal and spatial scales in the simulation are therefore directly comparable to those observed in the near-Earth space. The drawback to this approach is, however, the heavy computational cost of the runs, which have been so far limited to five dimensions, two in real space and three in velocity space (2D3V).

In this paper, we analyze two Vlasiator runs with identical setup, with the exception of the IMF strength, set to 5 nT in the first run, hereafter referred to as Run 1, and to 10 nT in the second run, Run 2. The IMF makes a 5° angle with the x axis, being in a so-called quasi-radial orientation. Consequently, the foreshock develops upstream of the subsolar bow shock and is particularly prominent in these conditions. The corresponding IMF components are $\mathbf{B}$(Run 1) = ($-4.98, 0.44, 0$) nT and $\mathbf{B}$(Run 2) = ($-9.96, 0.87, 0$) nT. Since the magnetic field is almost aligned with the solar wind flow, the solar wind motion electric field does not play a significant role in these runs. A first series of results from Run 1 has been presented in Palmroth et al. (2015), showing in particular that the simulation reproduces accurately the foreshock ULF wave properties. The following steady solar wind conditions are used in both runs: solar wind velocity $\mathbf{V} = (-600, 0, 0)$ km/s, ion density $n_{SW} = 3.3$ cm$^{-3}$, and ion temperature $T = 500$ kK. These parameters are representative of fast solar wind conditions encountered
regularly at Earth. The corresponding Alfvén Mach numbers are $M_A(\text{Run 1}) = 10$ and $M_A(\text{Run 2}) = 5$. The change in the IMF strength also affects the plasma $\beta$, that is, the ratio of the thermal pressure to the magnetic pressure, which is equal to 2.3 in Run 1 and decreases to 0.57 in Run 2.

The runs are 2-D in real space covering the $x$-$y$ plane, corresponding to the geocentric solar ecliptic (GSE) equatorial plane; all vector quantities will be given hereafter in this coordinate system, unless stated otherwise. A 3-D velocity space is self-consistently coupled with each ordinary space cell. The resolution in ordinary space is $\Delta r = 227$ km, that is, 1.8 solar wind ion inertial lengths, and in velocity space $\Delta V = 30$ km/s. The simulation box extends from $-7$ to $63.6 R_E$ along $x$ and $\pm 31.3 R_E$ along $y$. The solar wind flows into the simulation domain from the $+x$ boundary, while copy conditions are applied to the $-x$ and $\pm y$ walls, meaning that the VDFs and magnetic fields inside the boundary are copied from the nearest cell inside the simulation domain, thus ensuring a smooth outflow. The inner boundary is located at about 5 $R_E$ from the Earth’s center and is treated in these runs as a perfect conductor. The simulation was run for 685 s in Run 1 and 539 s in Run 2. As a side note, the quasi-identical setup of the two runs allowed us to assess the improvement of the code performance, as Run 1 was performed in 2014 and Run 2 in 2017. Run 2 ran about 2 to 3 times faster than Run 1, due to the implementation of more efficient solvers (Pfau-Kempf, 2016), thus showing the potential of Vlasia tor to eventually run in 6-D (i.e., 3D3V) with further improvements.

Previous studies have shown that Vlasia tor reproduces well ion acceleration in the foreshock (Kempf et al., 2015) and in the magnetosheath (Jarvinen et al., 2018), up to several tens of keV. Note, however, that to achieve global simulations, a sparse velocity grid has been implemented (von Alfthan et al., 2014), meaning that the most tenuous parts of the velocity space are discarded. The most energetic ions may therefore not be properly described. In terms of the wave frequency range, the main limitation comes from the spatial and temporal resolution of the simulation, which limit the steepening of the waves and the development of high-frequency oscillations such as the whistler wave packets commonly observed near the quasi-parallel bow shock (Pfau-Kempf et al., 2018). In the present study, we will therefore concentrate on waves at periods above 1 s, which are properly described in the current runs.

### 3. Results

#### 3.1. Large-Scale Structure of the Foreshock

Figures 1a and 1b show color maps of the plasma density in the simulation domain of Run 1 and 2 at $t = 500$ s from the beginning of the runs. This time step was selected because the foreshock is well developed but the waves have not yet reached the inflow boundary. Note that because of the 2-D configuration, the IMF piles up in front of the magnetosphere, causing the bow shock to move outward as time progresses. However, this effect is limited here because of the quasi-radial IMF configuration and takes place at comparable rates in both runs, thus allowing the comparison of the foreshocks at a given time in the simulation. The color scale is identical in both panels and has been chosen so as to best highlight the foreshock waves, which extend up to about $x = 60 R_E$. The white (panel a) and purple (panel b) contours are plotted where $n = 2n_{sw}$ and their rightmost part is a good approximation of the bow shock position. Figures 1a and 1b evidence that the overall structure of the foreshock differs strikingly from Run 1 to Run 2. In Run 1, the wave fronts are coherent over rather large distances perpendicular to the solar wind flow and are organized around two spines (Palmroth et al., 2015). In Run 2, however, the planar wave fronts are much smaller and the foreshock is structured at finer scales. This is probably related to the period of the foreshock waves being shorter in Run 2, as can readily be seen on these plots and will be analyzed in more detail in section 3.3.

In order to ease the comparison of the large-scale structure of the foreshock in the two runs, we plot in Figure 1c some of its characteristic features in both simulations, namely, the bow shock position (solid black and purple lines); the edges of the foreshock (dashed black and purple lines), that is, the limit of the region where field-aligned ion beams are observed; and contours of $B_x$ depicting the ULF foreshock. $B_x$ being set to 0 in the solar wind, the deviations from this value illustrate well the presence of foreshock waves. The contours are drawn at $B_x = 0.5$ nT (red and pink) and $B_x = -0.5$ nT (blue and green). The bow shock shape and position are similar in both runs, despite the fact that $M_A$ changes by a factor of 2. Previous works, based on magnetohydrodynamic (MHD) theory (Cairns & Grabbe, 1994) and simulations (Chapman & Cairns, 2004), have predicted that the bow shock position becomes less sensitive to changes in $M_A$ when $\Theta_{in}$ tends toward 0, and lower $M_A$ values have to be reached before the sunward retreat of the bow shock is observed. The similar bow shocks in our runs are thus due to the quasi-radial orientation of the IMF accompanied by rather high $M_A$ values. As $\Theta_{in}$ increases when moving toward the flanks, the bow shock of Run 2 lies there slightly farther...
Figure 1. (top panels) Ion density in the equatorial plane in Run 1 (a) and Run 2 (b) at time $t = 500$ s from the beginning of the runs. The color scale is chosen so as to best highlight the foreshock waves. The white/purple contours mark where $n = 2n_{SW}$ and illustrate the bow shock position. The plus signs indicate the positions of virtual spacecraft used in section 3.3. (c) Large-scale structure of the foreshock in both runs. Black and purple solid lines: bow shock position. Black and purple dashed lines: foreshock edge. Blue/red and pink/green contours: ultralow-frequency foreshock waves illustrated by contours of $B_z$ at $\pm 0.5$ nT.

From Earth than that of Run 1, consistent with the change in $M_A$. Our simulations thus support the predictions of MHD regarding the response of the quasi-parallel bow shock to changes in the upstream $M_A$.

Because of the comparable bow shock shapes in both runs, the edges of the foreshock (dashed lines in Figure 1c) are also very similar. This happens since the extent of the region where ion reflection occurs is controlled by $\Theta_{Bi}$. The foreshock is marginally broader in Run 2 due to the slightly flatter bow shock shape, thus enabling ion reflection over a somewhat larger area. This, however, does not seem to be sufficient to explain the difference in the extent of the ULF foreshock in the direction perpendicular to the solar wind flow, evidenced by the blue/red (Run 1) and green/pink (Run 2) contours, which is significantly larger than the variation of the position of the foreshock edges. The ULF foreshock develops upstream of the quasi-parallel shock, whose shape is essentially identical in both runs, thus ruling out the shock geometry as a sufficient explanation for the broader ULF foreshock in Run 2. Also, we note that the expansion of the ULF foreshock
into the upstream medium was faster in Run 2, reaching the inflow boundary of the simulation earlier than in Run 1 (not shown). This might be due to a difference in the growth rate of the instability giving rise to the ULF waves, which will be investigated in section 3.3.

3.2. Suprathermal Ion Properties
We now concentrate on the properties of suprathermal ions in the foreshock. The moments of the suprathermal population are direct outputs from our simulation. They are computed from the 3-D ion distribution function after excluding the solar wind core. This is done by removing the contribution of the part of the distribution function located within a sphere around the solar wind bulk velocity, with a 692.5 km/s radius that is well above the solar wind thermal velocity $V_{th} = 70$ km/s. The moments of the suprathermal population are therefore well defined in the field-aligned beam regions on either side of the foreshock, as the beam is distinct enough from the solar wind core. In the central foreshock, and even more so when moving closer to the bow shock, where the distribution functions become more complex, the moments of the suprathermal population should be used with more caution.

Figure 2a displays the ratio of suprathermal ion velocities in Run 1 and Run 2. In the outer foreshock (gray areas in the dawn ($y < 0$) and dusk ($y > 0$) sides of the foreshock), populated mostly by field-aligned beams, the velocity of suprathermal ions is essentially identical in both runs. This is consistent with models of generation of the field-aligned beams via reflection at the quasi-perpendicular bow shock (Burgess et al., 2012), as the beam energy then only depends on the inflow velocity and the geometry of the shock encounter (e.g., Schwartz et al., 1983). Here the solar wind velocity is the same in both runs, and the shock geometry varies very little, hence the comparable velocities. In the central foreshock, where ULF waves develop, the suprathermal ion velocity may be higher in Run 1, but part of the suprathermal population may not be taken into account in the moment calculation in this region. It is thus difficult to draw any conclusions as to the effect of the modified IMF strength on the suprathermal ions in the central foreshock without looking in more detail at the ion distribution functions.

The comparison of the suprathermal ion density ($n_{beam}$) in Run 1 and Run 2 is less straightforward. The ratio of this parameter in the two runs (Figure 2b) shows that in the outermost parts of the foreshock, the beam density is higher in Run 2 (in blue), while just outside of the ULF foreshock and in the central foreshock far from the shock, the opposite is observed (in green). To better illustrate the changes from one run to the other, we show the suprathermal ion density in Run 1 (Figure 2c) and Run 2 (Figure 2d). As the total ion density in Figures 1a and 1b, the color maps of suprathermal ion density reveal that the structuring of the foreshock operates at smaller scales in Run 2. Another major difference between the two runs is the bands of enhanced $n_{beam}$ that appear in Run 1 at the duskward and dawnward edges of the ULF foreshock (dark purple areas in Figure 2c) but are absent in Run 2. They are most prominent closer to the bow shock but remain visible throughout the simulation domain. These bands coincide with the green areas on either side of the central foreshock in Figure 2b, where the suprathermal ion density is a factor of 3 to 4 higher in Run 1 than in Run 2.

Figures 2e–2h show time-energy spectrograms at positions P1 and P2 in Run 1 (left) and Run 2 (right), where P1 is located in the region populated by field-aligned beams and P2 in the ULF foreshock (as marked in Figures 2c and 2d). On all spectrograms, the solar wind population is visible as a broad red band centered around 2 keV. The field-aligned beam appears as a blue band around 8 keV in panels e and g. Its energy decreases slightly as time proceeds because the foreshock edge moves outward as the foreshock develops. At position P2, the distribution of suprathermal ions is much broader, extending from a few tens of eV to tens of keV, consistent with the diffuse ion population observed deep in the ULF foreshock (Fuselier, 1995). We note that the solar wind core is partly disrupted. Furthermore, the flux of suprathermal ions is modulated. This is most visible between $t = 460$ s and $t = 490$ s in panel (f), corresponding to a period of about 30 s, but a modulation at a shorter period, around 10 s, may also be present in panel (h). This variation in the flux of suprathermal ions is similar to that reported by Petrukovich et al. (2015; see in particular Figure 4 of their paper) and is therefore likely caused by the foreshock ULF waves.

Figure 3a shows the suprathermal ion density along a cut perpendicular to the solar wind flow at $x = 30 R_E$, as depicted by the vertical lines in Figures 2c and 2d. When moving from the foreshock edge toward the central foreshock, in other words toward regions connected to more quasi-parallel shock configurations, the suprathermal ion density increases progressively in both runs (marked by the hatched black and purple bars), consistent with previous studies (see; Burgess et al., 2012, and references therein). The larger breadth of the foreshock in Run 2, as well as the slightly higher suprathermal ion density in the outermost regions, can most
likely be ascribed to the flatter bow shock shape, which results in the associated $\Theta_{Bn}$ being lower in Run 2 than in Run 1 at a given position in the foreshock. In Run 1 (black curve), the central foreshock is bounded by two ridges of higher suprathermal ion density, forming a peak and a plateau in the dawnward and duskward edges of the foreshock, respectively (indicated by the black bars in Figure 3a). These features correspond to the bands of enhanced $n_{beam}$ identified in Figure 2c. Inward of these ridges, the suprathermal ion density decreases toward the central foreshock. In Run 2, on the other hand, the smooth increase of $n_{beam}$ from the edge of the foreshock inward ends at a value comparable to that found in the central foreshock (purple curve).
Figure 3. From top to bottom: (a) suprathermal ion density, (b) total ion density, (c) magnetic field strength normalized to the IMF strength, and (d) $\delta B/B = |(B - B_{IMF})|/B_{IMF}$ in Run 1 (black) and Run 2 (purple) along a cut line through the foreshock at $x = 30R_E$. The black bars in panel (a) indicate the suprathermal ion ridges in Run 1, and the hatched bars show the regions where the suprathermal ion density increases progressively in Run 1 (black) and Run 2 (purple).

Figures 3b–3d display the total ion density, the magnetic field strength normalized to the IMF strength $B/B_{IMF}$, and the amplitude of the fluctuations of $B$, $\delta B/B = |(B - B_{IMF})|/B_{IMF}$. These parameters all indicate that the suprathermal ion ridges are located just outside of the region of the foreshock populated by highly compressive waves. This is particularly well illustrated by $\delta B/B$ which increases significantly in the inner part of both ridges. We also note that when entering the foreshock from the duskward edge, we observe correlated enhancements in the magnetic field magnitude and plasma density, which then decrease below their initial values. This is consistent with the crossing of the foreshock compressional boundary, which marks the entry into the region of the ULF foreshock where compressive waves develop (Kajdič et al., 2017; Omidí et al., 2009; Rojas-Castillo et al., 2013). We propose the following scenario for the formation of the ridges. As mentioned above, the density of field-aligned beams increases when moving toward smaller $\Theta_{Bn}$ values. At some point, ULF waves start to develop from the ion-ion beam instability and alter in return the suprathermal ion population. Small-amplitude waves only weakly modify the ion distribution functions, thus creating the plateau-like structure in the duskward foreshock. However, as the waves become more compressive, they scatter much more efficiently the ions and result in a decrease of the suprathermal ion density toward the central foreshock. Because the amplitude of the waves is larger closer to the edge of the dawnward foreshock, only a peak and not a plateau is observed there.

Clearly, the variation of the IMF strength affects the development of this ridge of suprathermal ions at the edge of the ULF foreshock. The different Mach numbers and plasma $\beta$ imply that the shock structure differs between the two runs. This is also expected to affect the fraction of shock-reflected ions, resulting in a higher suprathermal ion density in Run 1 than in Run 2 for a given $\Theta_{Bn}$. This explains the much larger $n_{beam}$ at the edge of the ULF foreshock in Run 1. Furthermore, Figure 3d shows that the amplitude of the ULF waves is significantly lower in Run 2 and is roughly the same across the ULF foreshock. We do not observe clear signatures of the foreshock compressional boundary, in agreement with the work by Omidí et al. (2009), which showed that it becomes weaker when the Mach number decreases and thus implies that the foreshock waves become less compressive. Therefore, with only small-amplitude waves throughout the ULF foreshock, the suprathermal
ions would not experience increased scattering in the central foreshock, which could explain the relatively constant $n_{\text{beam}}$ along the cut through the foreshock in Run 2 (see the purple line in Figure 3a).

### 3.3. Foreshock Wave Properties

To investigate the foreshock ULF wave properties, we extract time series of data at 30 locations in the foreshock indicated by the plus signs in Figures 1a and 1b. We apply a wavelet transform (Torrence & Compo, 1998) using a Morlet mother waveform to each magnetic field component of each time series. The wavelet transform was chosen because it allows to investigate the temporal variation of the wave activity. We then compute the total power spectrum density (PSD) of the fluctuations, as defined, for example, in Perrone et al. (2016). The peaks of the PSD yield the period of the dominant wave modes, while the wavelet power spectra show how these evolve over time. As an example, Figures 4a–4c showcase the $B_z$ component of the magnetic field at the virtual spacecraft A located at ($x = 35\,R_E, y = -10\,R_E$) in Run 1, its color-coded wavelet power spectrum as a function of time and period, and the total PSD over the entire considered interval. The hatched part of the wavelet power spectrum corresponds to the region below the cone of influence, where edge effects become important, and is thus not taken into account when computing the PSD. Black contours indicate the 95% confidence level. The wavelet power spectrum in Figure 4b shows that there is essentially one predominant wave mode, with a period of about 34 s according to the PSD, corresponding to the 30-s foreshock waves (Eastwood, Lucek, et al., 2005), as was already shown in Palmroth et al. (2015).

#### 3.3.1. Wave Modes

The distribution of the number of wave modes in the foreshock is illustrated in Figures 1a and 1b, where the white and pink plus signs indicate single-peaked and double-peaked $B_z$ PSD, respectively. Secondary peaks are considered significant when they reach at least 40% of the maximum PSD, as was done in Palmroth et al. (2015). In Run 1, the wavelet spectrograms and associated PSD obtained for each of the virtual spacecraft indicated in Figure 1a reveal that the foreshock is mostly permeated by quasi-monochromatic waves.

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**Figure 4.** Wave activity at ($x = 35\,R_E, y = -10\,R_E$) in Run 1. From top to bottom: (a) time series of the magnetic field $B_z$ component, (b) its associated wavelet power spectrum, and (c) total power spectrum density over the whole interval. The black contours in panel (b) outline the 95% confidence level, while the hatched area is below the cone of influence.
Figure 5. Wave activity at \((x = 25R_E, y = -10R_E)\) in Run 2. (a) time series of the magnetic field \(B_z\) component, (b) its associated wavelet power spectrum and (c) total power spectrum density over the whole interval. Hodograms of the waves in the plane perpendicular to the wave vector between \(t = 350\) s and \(t = 400\) s (d) and \(t = 480\) s and \(t = 510\) s (e) and ion velocity distribution functions at times \(t = 350\) s (f) and \(t = 480\) s (g). In panels d and e, the average magnetic field is pointing toward the reader. The black bars in panel (a) indicate the intervals on which minimum variance analysis is applied and from which panels (d) and (e) are constructed.
atevariancedirectionsaredegenerate. Wefindthatthe17-swavespropagateatabout30° direction,iswelldefined (Eastwood, Balogh, et al., 2005b). Note,however,thatthemaximumandintermediate eigenvalues is above 10, meaning that the minimum variance direction, which is the wave vector corresponding to one of the wave modes being dominant. For both intervals, the ratio of intermediate to minimum variance direction of the wave vector on two subintervals, depicted by the black rectangles in Figure 5a, each corresponding to one of the wave modes being dominant. For both intervals, the ratio of intermediate to minimum eigenvalues is above 10, meaning that the minimum variance direction, which is the wave vector direction, is well defined (Eastwood, Balogh, et al., 2005b). Note, however, that the maximum and intermediate variance directions are degenerate. We find that the 17-s waves propagate at about 30° from the magnetic field direction, while the 10-s waves are more parallel-propagating, with a propagation angle of about 6°. We then project the magnetic field into a frame defined by the wave vector $\mathbf{k}$ and two perpendicular directions forming a right-handed triplet and plot its two perpendicular components as a function of each other, in order to examine the polarization of the waves. Figures 5d and e reveal that the waves are left-handed in the simulation frame during both intervals. This polarization is consistent with that of magnetosonic waves generated by the ion-ion beam right-hand instability which propagate toward the upstream parallel to the beam and therefore appear as left-handed in the simulation frame (Hoppe & Russell, 1983). This suggests that the same type of instability generates magnetosonic waves with two different periods. The resonance condition of this mode is given by

$$\omega = V_{\text{beam}} k_\parallel - \Omega_{ci}$$

(1)

where $V_{\text{beam}}$ is the beam velocity and $\Omega_{ci}$ is the ion gyrofrequency, showing that the period of the waves is mainly controlled by the beam speed (see, e.g., Eastwood, Balogh, et al., 2005b).

Figures 5f and 5g display two ion VDFs taken at $(x = 24.3 R_E, y = -9.8 R_E)$, which is the nearest cell to virtual spacecraft B where VDFs were recorded, at two different times in the run. The phase space density in the $(V_\parallel, V_\perp)$ plane (relative to the magnetic field) is color-coded, computed from the 3-D VDF as it was scanned by the electrostatic analyzer (McFadden et al., 2008) onboard the THEMIS satellites (Angelopoulos, 2008), in order to facilitate comparison with typical VDFs in spacecraft measurements. To do so, we consider that the spin axis of the spacecraft is normal to the $(V_\parallel, V_\perp)$ plane, and we integrate the phase space density within the 6° opening angle of the instrument. Figure 5f, at $t = 350$ s, showcases a typical field-aligned beam, with the solar wind core on the left side of the plot. This distribution coincides with the time when a single wave mode starts to develop at virtual spacecraft B. As time proceeds, the beam parallel velocity decreases, likely because of energy loss through the production of ULF waves, while a second beam, with a higher parallel speed, appears and grows. At $t = 480$ s, when the wave activity is stronger and covers a broad range of periods, with two peaks around 10 and 17 s (see Figure 5b), the VDF comprises two populations of backstreaming suprathermal ions. Because of their different parallel velocities, each of these beams may excite magnetosonic waves at different frequencies through the right-hand resonant ion-ion beam instability (see equation (1)). Closer to the bow shock ($x \lesssim 20 R_E$), the VDFs display the characteristics of intermediate or diffuse distributions, covering a much broader range of pitch angles (not shown). Therefore, some of the waves observed there might be caused by other instabilities. In particular, spacecraft observations have shown that other types of waves,
such as Alfvén modes, can develop in conjunction with diffuse ions (Eastwood et al., 2003). In Run 1, the only location at which two modes are present is also associated with intermediate ion distributions. Further out in the foreshock, we mostly encounter field-aligned beams, with only one suprathermal ion population. This may explain why only quasi-monochromatic waves permeate the foreshock in Run 1, while they develop at multiple frequencies in Run 2.

In order to check whether two beams at different parallel velocities can excite magnetosonic waves with distinct frequencies, we use the Waves in Homogeneous Anisotropic Magnetized Plasmas code (WHAMP, https://github.com/irfu/whamp, Kempf et al., 2013; Rönnmark, 1982) to characterize the fastest-growing wave modes. We use as inputs to the code three ion populations: one with parameters representative of the inflow-solar wind and two corresponding to the two beams in Figure 5, with velocities $V_{\text{beam 1}} = 400$ km/s and $V_{\text{beam 2}} = 1,200$ km/s and densities $n_{\text{beam 1}} = 7 \times 10^3 \text{ m}^{-3}$ and $n_{\text{beam 2}} = 3 \times 10^3 \text{ m}^{-3}$. We find that the maximum growth rate of the waves is in the $k_\parallel$ direction. Figure 6 shows the dispersion relation obtained from WHAMP in the $(\omega, k_\parallel)$ plane. The color scheme indicates the growth rate and shows that it maximizes in two parts of the dispersion relation, around $\omega/\Omega_{ci} = 0.3$ and $\omega/\Omega_{ci} = 0.55$. This corresponds to periods of 21 and 12 s, respectively. This is comparable to the periods of the waves found in the simulation, which supports our interpretation that the multiple ion beams are the source of the magnetosonic waves at different frequencies.

### 3.3.2. Wave Periods

In order to compare our simulation results with observations, we calculate the average period of the dominant wave mode in the foreshock. To do so, we extract the period associated with each significant peak of the PSD for all 30 virtual spacecraft and all three magnetic field components. This allows us to build histograms of the wave periods for both runs, which are shown in Figure 7. The variation of the wave period within the foreshock, despite the steady upstream conditions, is due to the variability of the beam velocity (Palmroth et al., 2015). The median periods are very similar for all three components in a given run, about 36 s in Run 1 and 16 s in Run 2. The period of the waves is thus roughly divided by 2 when doubling the IMF strength, consistent with early spacecraft observations (Hoppe & Russell, 1982). Note that we included here all significant peaks of the PSD. Retaining only the dominant period at each virtual spacecraft led to changes of less than 1 s in the median periods. The empirical formula derived by Le and Russell (1996), $f(\text{mHz}) = (0.72 + 4.67 \cos \theta_{\parallel}) B (\text{nT})$, yields the following predicted periods: $T(\text{Run 1}) = 37$ s and $T(\text{Run 2}) = 19$ s, which are very close to our results. The wave periods estimated using the Takahashi et al. (1984) model $\omega = -\Omega_{ci}(1 - M_\parallel \cos \theta_{\parallel})/(1 - 2M_\parallel \cos \theta_{\parallel})$ are $T(\text{Run 1}) = 28$ s and $T(\text{Run 2}) = 15$ s. These are slightly lower than in our simulation for Run 1 but still in reasonable agreement. This slight discrepancy might be due to the fact that the foreshock waves are assumed to be generated by protons reflected at the bow shock nose in the Takahashi et al. (1984) model, whereas particle reflection occurs over a large fraction of the bow shock in our simulations. Overall, the evolution of the periods of the foreshock waves as a function of the IMF strength is well reproduced by our model.

### 3.3.3. Growth Rate

As mentioned in section 3.1, the foreshock appears to be broader in Run 2 than in Run 1. This might be due to a larger growth rate of the foreshock waves in Run 2, since the growth rate of the waves affects the location of the foreshock ULF boundary (Eastwood, Lucek, et al., 2005). The field-aligned beams would then need to travel a shorter distance before the waves grow significantly. The earlier development of the waves would result in the ULF foreshock extending farther out. In order to test this hypothesis, we evaluate the growth rate of the magnetosonic waves as they are the predominant wave mode across the foreshock. This parameter can be estimated in the simulation at the time when the waves start to appear at a given location in the foreshock. As was done for the wave period, we extract time series of the magnetic field fluctuations at different locations in the foreshock. Since we focus here on the 30-s waves, we exclude the region close to the bow shock where other wave modes can also develop ($x < 30 R_E$). Furthermore, we require that the waves are nearly sinusoidal when they start to grow and that they display at least five consecutive extrema with increasing amplitude (in absolute value), in order to obtain a reasonable fit quality when estimating the growth rate.
Figure 7. Histograms of the wave periods in Run 1 (green) and Run 2 (purple), as obtained from a wavelet transform applied to the magnetic field $B_x$ (a), $B_y$ (b), and $B_z$ (c) components. The median period $\bar{T}$ and its associated standard deviation $\sigma$ in each run are indicated on the panels.

We then perform a minimum variance analysis on the magnetic field time series of each virtual spacecraft and retain those for which the determination of the minimum variance direction was reliable, that is, when the ratio of intermediate to minimum eigenvalues was larger than 10 (Eastwood, Balogh, et al., 2005a). The magnetic field components are calculated in the minimum variance frame, where $B_n$ is parallel to the wave vector (minimum variance direction) and $B_l$ and $B_m$ along the maximum and intermediate variance directions, respectively. The sinusoidal waves being essentially transverse (Blanco-Cano et al., 2006; Le et al., 1992), we use the $B_l$ and $B_m$ components to determine the growth rate, as exemplified in Figure 8 with the $B_l$ component at position ($x = 35 R_E$, $y = 5 R_E$) in Run 1. We identify the extrema of the magnetic field component time series (red plus signs) until the amplitude of the wave stops increasing and fit their absolute values with an exponential function, $\exp(\gamma t)$, where $t$ is the time and $\gamma$ the growth rate (blue curve in Figure 8b). The quality of the growth rate estimate is evaluated using the 95% confidence interval. If the length of the 95% confidence interval is greater than 50% of the value of the growth rate, we consider that the growth rate is not reliable and discard it.

Histograms of the growth rates thus obtained in the foreshock of Run 1 (in green) and Run 2 (in purple) are displayed in Figure 8c. The median growth rate in Run 1 is $0.019 \text{ s}^{-1}$ and $0.037 \text{ s}^{-1}$ in Run 2, that is about 1.9 times higher. This could then explain the broader ULF foreshock in Run 2. Gary (1993) has shown that
Figure 8. Growth rate of the foreshock waves. (a) Time series of the magnetic field $B_l$ component, as determined from minimum variance analysis, at $(x = 35 R_E, y = 5 R_E)$. The red plus signs indicate the extrema of the fluctuations with increasing amplitude. (b) Fit of the extrema of $B_l$ as a function of the growth rate $\exp(\gamma t)$. (c) Histograms of the growth rates in Run 1 (green) and Run 2 (purple). The median growth rate $\bar{\gamma}$ and its associated standard deviation $\sigma$ in each run are indicated.

The maximum growth rate $\gamma_m$ of the ion-ion right-hand resonant instability, in the direction parallel to the magnetic field, is

$$\frac{\gamma_m}{\Omega_{ci}} = \left( \frac{n_b}{2n_e} \right)^{1/3}$$

where $\Omega_{ci}$ is the plasma gyrofrequency, $n_b$ the beam density, and $n_e$ the electron density. $\Omega_{ci}$ is twice as large in Run 2 than in Run 1 because the IMF strength is doubled, while the beam density is about 2 to 3 times lower in the region where the waves start to develop (see Figure 2b), which corresponds to the outer parts of the ridges we investigated in section 3.2. According to equation (2), the growth rate should therefore be 1.4 to 1.6 larger in Run 2 than in Run 1. Our estimate of the variation of the growth rate from one run to the other
is therefore in reasonable agreement with theoretical expectations. The discrepancy might be due to the fact that the formula established by Gary (1993) is valid for beam densities ranging between 1% and 10% of the total ion density, whereas they are below 1% at the locations where the growth rate was determined. Also, the growth rate varies significantly across the foreshock, in particular in Run 2 (see Figure 8c), due to larger variations in the suprathermal ion density. This can also introduce errors in the estimate of the growth rate variation from Run 1 to Run 2.

A recent study by Dorfman et al. (2017) provides an observational estimate of the growth rate of the ULF waves in the terrestrial foreshock, using data from the ARTEMIS mission around the Moon (Angelopoulos, 2011). The spacecraft, initially located outside of the foreshock, moved inside the ULF foreshock after a change in the IMF direction. From the variation of the amplitude of the waves from one satellite to the other, Dorfman et al. (2017) estimated the growth rate to be $\gamma/\Omega_{ci} = 0.035$. The median normalized growth rates in our simulations, $\gamma/\Omega_{ci} = 0.042$ for Run 1 and $\gamma/\Omega_{ci} = 0.041$ for Run 2, are very comparable to the observational estimate, despite the very different solar wind conditions at the time of ARTEMIS measurements.

4. Summary and Discussion

In this paper, we have presented a detailed study of the effects of the IMF strength on the foreshock properties using global hybrid-Vlasov simulations. As expected from early spacecraft observations at different planetary foreshocks, the frequency of the ULF waves is roughly proportional to the IMF strength (Hoppe & Russell, 1982), resulting in wavelengths halved in Run 2 compared to Run 1. The modification of the wave frequency can have a direct impact on the wave activity inside the magnetosphere because foreshock ULF waves are thought to be the main source of magnetospheric Pc3 – 4 pulsations (Francia et al., 2012; Takahashi et al., 1984; Villante et al., 2011). Furthermore, the transverse extent of the wave fronts is much smaller when the wavelength is shorter. The shock rippling, which is known to be modulated by the foreshock ULF waves (Burgess, 1995; Greenstadt & Mellott, 1985), may therefore occur at smaller scales in Run 2. This is probably interconnected with the structuring of the foreshock around the so-called spines, where the obliquity of the waves changes. The spines being more numerous and more closely spaced in Run 2, the wave fronts are smaller.

The change in the IMF strength also affects the growth rate of the instability which triggers the magnetosonic waves permeating most of the foreshock. The broader foreshock in Run 2 implies that a larger fraction of the magnetosheath, and therefore of the magnetosphere, is located downstream of the ULF foreshock. Russell et al. (1983) have shown that waves reaching the subsolar magnetopause propagate to lower $L$ values than those reaching other parts of the magnetopause. For a quasi-radial IMF orientation as presented here, the broadening of the foreshock may not affect significantly the transmission of the fluctuations into the inner magnetosphere because the foreshock is upstream of the subsolar point. However, for other IMF orientations, a broader ULF foreshock may extend to magnetosheath streamlines connected with the subsolar region, thus allowing the waves to be transmitted deeper into the magnetosphere when the IMF strength is enhanced.

We found that at higher IMF strength, magnetosonic waves can develop at distinct frequencies in some parts of the foreshock. This was attributed to the presence of several backstreaming populations with different velocities. This is further supported by the results from the WHAMP code with two backstreaming ion beams. The origin of the second population, while only one beam is seen in Run 1, is however not completely clear. They may either be generated already at the bow shock, from a second reflection at the shock surface after having been advected back to it, or result from wave-particle interactions in the foreshock. The different plasma $\beta$ in the two runs may play a role in this, as they result in different shock properties, which could affect the generation of field-aligned beams. Meziane et al. (2011) reported observations from the Cluster spacecraft of multiple field-aligned beams resembling those in our simulation. The authors suggested that the anomalous population could be produced by local changes of the quasi-parallel shock surface due to foreshock ULF waves or plasma structures. This could be further investigated in our runs but lies beyond the scope of this paper.

Additionally, we found that the bow shock shape and position change very little from one run to the other. This is attributed to the quasi-radial IMF orientation and the relatively high Mach numbers and is consistent with MHD predictions. This suggests that despite kinetic effects being prominent in the quasi-parallel shock regime, they may not affect significantly the overall shock position and shape, and an MHD description may be sufficient to capture them. The similar bow shocks facilitated the comparison of the two simulation runs, but it would be interesting to investigate the response of the bow shock for different IMF orientations. A preliminary
analysis of another set of runs with more oblique IMF compared to that analyzed here confirmed that the quasi-perpendicular bow shock retreats farther sunward than its quasi-parallel region when decreasing the $M_b$ (not shown).

Finally, we identified new large-scale foreshock structures, namely, two bands of enhanced suprathermal ion density flanking the central foreshock, and proposed a scenario to explain their formation. In these structures, the suprathermal ion density is maximized because of the value of the $\Theta_{IN}$ angle at the bow shock, while we attribute the decrease of suprathermal ion density in the central foreshock to enhanced scattering due to the compressional waves found in this region. They seem to be colocated with the foreshock compressional boundary (Omidi et al., 2009), and their disappearance at lower $M_b$ further supports that they are another signature of the same phenomenon, previously undetected because the suprathermal ion density is not readily obtained from spacecraft data. Revisiting the observed crossings of the foreshock compressional boundary could test this hypothesis.

Despite being restricted to 2-D in real space, our simulation results show very good agreement with previous studies, suggesting that the addition of a third dimension would not change fundamentally the main foreshock properties in the simulation. Since no comparative study of 2-D and 3-D simulations of the foreshock has been carried so far, estimating how the 3-D would affect them precisely can only be speculative. It is however expected that the wave activity will become even more complex in 3-D.

In conclusion, a change in the IMF strength alters significantly the foreshock properties at both large and small scales, which can in turn affect the regions downstream of the quasi-parallel shock. The wave properties are of particular importance because foreshock fluctuations can be transmitted into the inner magnetosphere. The enhanced IMF case studied here is representative of the magnetic field strength encountered during interplanetary coronal mass ejections or magnetic clouds. It can be regarded as a snapshot of the foreshock during such an event, since the solar wind parameters are generally quasi-steady inside these transients, even though it must be noted that not only the IMF strength changes during such events. This suggests that the foreshock can differ significantly from its normal state in these conditions. High IMF strengths can also be typical solar wind conditions for other planets such as Mercury or exoplanets orbiting close to their host star. The present study can therefore serve as a basis to understand other planetary foreshocks and may for example help interpret the data from the upcoming BepiColombo mission at Mercury.

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