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Facet Growth of $^4$He Crystals at mK Temperatures


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We have investigated growth of facet crystals in good quality helium crystals with screw dislocation densities $0–20$ cm$^{-2}$ along the $c$ axis. Three distinct regimes of growth were observed. One of them can be explained by spiral growth provided that kinetic energy of moving steps and their tendency to localization at large driving forces are taken into account. In the absence of screw dislocations we find burstlike growth unless the speed is less than 0.5 nm/s, in which case anomalous, intrinsic growth of facets is detected. [S0031-9007(96)00296-7]

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The interface between the liquid and solid phases of helium provides a unique object to investigate interfacial physics in a situation where thermal processes do not disturb the kinetic behavior of basic surface excitations. Owing to the quantum nature of helium crystals, elementary kinks on an atomic step can be regarded as quasiparticles, moving freely along the step [1]. Highly mobile kinks and steps have provided the standard framework for theoretical description of interfacial phenomena in helium [2–4]. Typically, such a description has been very successful in explaining experimental results, e.g., crystallization waves in $^4$He [5]. First indications of subtle deficiencies in the standard theoretical treatment were obtained recently in high-resolution interferometric experiments performed on static properties of crystal facets [6]. In this Letter we present data which show that striking shortcomings in the theoretical understanding appear also when dynamic properties of facets are investigated.

We have studied the growth of facets in $^4$He crystals at mK temperatures. Typically, the growth of facets at low temperatures is assigned to the presence of screw dislocations [7,8]. Our results indicate, however, that growth is possible also in crystals with no screw dislocations at all along the $c$ axis. In such crystals novel mechanisms are needed for growth. Our experiments show that there are two mechanisms present at low temperatures: One, continuous at small interface speeds, and another, burstlike at larger speeds. Both mechanisms are found to become increasingly effective with lowering temperature below 0.3 K.

In these investigations we employed two-beam optical interferometry developed in our laboratory for experiments at ultralow temperatures [9]. In the present work, our interferometric resolution for the position of the liquid-solid interface was well below 10 nm, which was obtained using the Fourier method described by Kostianovski, Lipson, and Ribak [10]. The experimental chamber was a polished copper cylinder ($\phi = 17$ mm, height $= 18$ mm) with the upper end sealed with a fused silica window whose normal is tilted by $2^\circ$ off the cylinder axis. The lower end was closed by a MgF$_2$-coated fused silica wedge acting as our optical reference flat. The cell was connected to a copper nuclear demagnetization stage via a sintered silver heat exchanger with 100 m$^2$ surface area; the total liquid volume of the setup was 20 cm$^3$. Temperatures were measured using a Pt-wire NMR thermometer mounted on the top flange of the nuclear stage ($T = 0.3–70$ mK) and with a carbon resistor located on the mixing chamber (20–300 mK). On the basis of previous experiments by van de Haar $et$ $al.$ [11] we expect that the lowest temperatures reached in our experiments are around 2 mK, although the nuclear stage was cooled down to 0.3 mK in some of the runs. The basic heat leak to the nuclear stage was about 30 nW. The rate of pulsed light was varied in the range of $f = 0.01–3$ Hz which resulted in heat leaks of 0.02–6 nW to the sample owing to light absorption on the windows. Pressure was measured using a Straty-Adams type capacitive gauge having a resolution of 0.3 $\mu$bar.

The crystals were grown using regular commercial helium with nominal purity of $10^{-7}$. The $c$ facets of our crystals were aligned almost parallel to the upper surface of the optical reference wedge ($\Delta\phi \approx 10$ mrad), by following the recipe described in the Ref. [12]; in these experiments, however, we did not use any high electric field to enhance the pressure locally. Our crystals were nucleated at 20 mK by pressurizing the liquid slowly from a gas ballast at room temperature. First, we generated a suitable seed: the compression of the liquid was commenced 0.8 bar below the melting curve which was a sufficiently low starting point so that a crystal nucleated in a quite random position on the wall at an overpressure of about 3 mbar. After a few seconds the nucleated crystal either dropped to the bottom or started sliding down along the wall. By monitoring the pressure change as a function of time we could see from which height the crystal dropped. If the height was larger than 5 mm and the detached crystal landed almost horizontally, the seed was regarded as suitable. By keeping the pressure thereafter within a few millibars of the melting curve, all the subsequent crystals nucleated in the same place and dropped in a similar fashion. About twenty tries
were typically sufficient to generate a crystal with a proper orientation so that interference fringes could be observed. After nucleation the crystal was grown slowly (1 \(\mu\)m/s) across the bottom by heating a 100 cm\(^3\) gas ballast on top of the cryostat.

Growth of \(c\) facets was investigated in vertical motion at velocities \(v = 0.01\) nm/s–50 \(\mu\)m/s. The movement of the interface could be measured either by tracing the interference lines (\(v = 0.01\)–50 nm/s) or by using the pressure of the liquid as a level gauge (\(v = 0.05\)–50 \(\mu\)m/s). A typical \(p\) vs \(t\) plot for an advancing \(c\) facet is shown in Fig. 1(a) where the crystal is grown vertically at an average speed of 170 nm/s. The curve shows several, almost linearly increasing sections which are abruptly cut off at irregularly located points of instability. At the instability points the pressure decreases almost instantaneously down to 100 \(\mu\)bar which, according to the compressibility of the liquid, corresponds to a sudden, rapid growth of the crystal by 200–2000 layers.

During the sections of growing pressure in Fig. 1(a), there is, in fact, a slow, continuous movement of interference lines. This could be seen more reliably by stabilizing the driving pressure below the instability region. The rate for the slow growth as a function of pressure is illustrated in Fig. 2. The rate varies in the range 0–0.5 nm/s, and it increases towards decreasing temperatures. Within our accuracy the velocity data can be fitted by a linear dependence \(v = \mu_f f\), where \(\mu_f\) denotes the facet mobility and the driving force is defined as \(f = a(\Delta p/\rho_f)\Delta p\); here \(\rho = 3 \times 10^{-8}\) cm is the interatomic spacing, \(\Delta p = \rho_s - \rho_f\) is the difference between solid and liquid densities, and \(\Delta p = p - p_{eq}\) denotes the pressure deviation from the equilibrium. The resulting facet mobility \(\mu_f(T)\) in illustrated in the inset of Fig. 2.

We argue that the above behavior is intrinsic for crystals without any screw dislocations along the \(c\) axis. We were able to generate screw dislocations in our experiments by growing crystals horizontally at a few hundred \(\mu\)m/s or vertically at about 1 \(\mu\)m/s when \(T \sim 200\) mK. In the latter case, the distribution of measured instability pressures extended above 3 mbar which was a typical value for creating new crystals in our experimental chamber. According to the interference fringes, the orientation of the crystal did not change upon such an event but screw dislocations were created, which was seen as a dramatic increase in the growth rate and as a reduction of the growth threshold \(\Delta p_c\) down to about 1 \(\mu\)bar. The dislocations could be eliminated by melting the crystal below its size in the original creation process.

Growth of a crystal with a small threshold is illustrated in Fig. 1(b) which displays one cycle of a sinusoidal growing and melting sequence. Initially, when helium feed to the cell is started, no growth of the facet is observed, just a gradual increase in the pressure. The growth threshold \(\Delta p_c = 2\) mbar is exceeded at point \(P\) where the movement of fringes begins. The slight increase in the excess pressure (~1 \(\mu\)bar) after point \(P\) is identified as originating from the force needed to get the interface moving at the wall; this extra pressure is seen to diminish
slightly when the interface is moving. The threshold of 2 μbar is also seen as a stationary section between growth and melting.

The growth threshold for a facet is related to the density of dislocations by the formula [4,13] \( \Delta p_c = (\rho / \Delta \rho) \times 2 \beta / l \), where \( \beta = 0.014 \text{ erg/cm}^2 \) [14] is the step energy and \( l \) is the average distance between neighboring screw dislocations of different sign. Hence, our smallest growth threshold \( \Delta p_c = 0.5 \mu \text{bar} \) corresponds to a density of dislocations \( n_s = 5 \text{ cm}^{-2} \). Our values are smaller by an order of magnitude than the previous densities reported by Lenga and Goodkind [15] and by Rolley et al. [14].

The velocity of facets measured in a crystal with \( \Delta p_c = 0.5 \mu \text{bar} \) is displayed in Fig. 3. The data at \( T = 100 \), 150, and 200 mK can be fitted quite well by the classical \((\Delta p)^2\) power law [4] up to velocities 30 μm/s. At \( T = 2-20 \text{ mK} \), on the other hand, the dependence on pressure is nearly linear within our resolution. In all sets of data, deviations from the initial pressure dependence are observed at large velocities. A hint of the physical reason for these deviations from the \((\Delta p)^2\) power law can be obtained from the estimation of the step velocity \( v_s \). This speed is related to the facet velocity by the formula \( v = (a / d) v_s \), where \( d \) is the spacing of the spiral arms. Using \( \Delta p = 2 \mu \text{bar} \), \( v = 10 \text{ μm/s} \), and \( d = 20(\rho / \Delta p) \beta / \Delta p \) (valid for classical spiral growth) we obtain \( v_s = 300 \text{ m/s} \), i.e., a value which equals the sound velocity in helium. At such large velocities the standard theory of spiral growth [4] is not sufficient and modifications of the calculation are needed.

In our modified theory of spiral growth two new features have been taken into account: step inertia and localization of steps at large driving forces. The equation of step motion can be written in the form

\[
m(\partial v_s / \partial t + v_s \partial v_s / \partial n) = f - \beta^* a / \bar{r} - v_s / \mu,
\]

where \( m \) is the effective mass of a step per unit length, \( n \) is normal to the step, \( \beta^* a = \beta a + mv_s^2/2 \) denotes the step energy including the kinetic energy, \( \bar{r} \) is the radius of curvature of the step at a given point, and \( \mu \) is the step mobility. Stationary solutions of Eq. (1), corresponding to growth of the whole facet with constant velocity \( v \), were obtained numerically.

At low temperatures, where the mobility of steps is large, \( v_s = \mu f \) as before, but the asymptotic spacing of the spiral arms \( d = \pi \mu(2mA\beta)^{1/2} \) differs from its classical value, which leads to a linear velocity versus pressure dependence as seen in the experiments. From the data in this limit we may estimate the step mass \( m = (4 - 5) \times 10^{-18} \text{ g/cm} \) which is in a good agreement with the theoretical value [3,16] \( m = (5 - 7) \times 10^{-18} \). At higher temperatures, Eq. (1) yields the regular \((\Delta p)^2\) dependence.

In the “inertial” limit (\( \mu \to \infty \)) with constant values of \( m \) and \( \beta \), Eq. (1) predicts a temperature independent velocity \( v \). However, the experimental values of \( v \) in Fig. 3 decrease significantly at higher temperatures. In addition, the measured velocities display a tendency to saturation above 40 μm/s. This can be viewed as an indication of localization under large driving forces [17]. Such a behavior is expected for quantum systems with narrow-band quasiparticles, like kinks on a step [1]. As long as kink movement implies the motion of steps, localization of kinks might result in localization of the step itself. In the regime of localization, the speed of a step is inversely proportional to the driving pressure and the mobility can be expressed as

\[
1 / \mu = 1 / \mu_0 + \eta f^2,
\]

where \( \mu_0 \) is the step mobility at small speeds and \( \eta \) is a parameter describing energy relaxation of “localized” steps. Fitting of this formula to the experimental data in the range \( T = 50-200 \text{ mK} \) yields a temperature independent value \( \eta = 3 \times 10^2 \); at low temperatures \( T = 2-20 \text{ mK} \) a reasonable agreement is also obtained with this value. Solid lines in Fig. 3 illustrate the good quality of our theoretical fits for spiral growth obtained with Eqs. (1) and (2) using the step mobility \( \mu_0 \) as a fitting parameter at constant \( \eta = 3 \times 10^2 \) and \( m = 5 \times 10^{-18} \text{ g/cm} \).

Temperature variation of the burstlike growth mechanism without screw dislocations is illustrated in Fig. 4 which displays cumulative distributions of instability pressures at three different temperatures. These distributions were measured at an average interfacial velocity of 200–300 nm/s but no variation as a function of speed was observed in the range 100–600 nm/s. With increasing temperature the asymmetry of the distributions about their median values becomes more prominent. In general, the functional shapes agree with expectations for thermal and quantum tunneling [18].

The inset of Fig. 4 displays the temperature dependence of the median pressures taken from the measured distributions. There is an increase by a factor of 3 in the median pressure when \( T \) is increased from 20 to 200 mK; i.e.,
After adding superfluid, the system displays a strongly temperature dependent distribution. At small speeds up to 0.5 nm/s, we observe anomalous, slow facet growth, approximately linearly dependent on the driving pressure.

In conclusion, we have shown that it is possible to generate very good crystals by nucleation at 20 mK in the absence of pressure gradients. We have identified three different regimes for crystal growth at ultralow temperatures. One of them can be assigned to the screw-dislocation-mediated spiral growth provided that inertial and localization effects are taken into account. In the absence of screw dislocations, facet growth is typically made of consecutive jumps whose occurrence in pressure displays a strongly temperature dependent distribution. At small speeds up to 0.5 nm/s, we observe anomalous, slow facet growth, approximately linearly dependent on the driving pressure.

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