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Start-up inertia as an origin for heterogeneous flow

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For quite some time nonmonotonic flow curve was thought to be a requirement for shear banded flows in complex fluids. Thus, in simple yield stress fluids shear banding was considered to be absent. Recent spatially resolved rheological experiments have found simple yield stress fluids to exhibit shear banded flow profiles. One proposed mechanism for the initiation of such transient shear banding process has been a small stress heterogeneity rising from the experimental device geometry. Here, using computational fluid dynamics methods, we show that transient shear banding can be initialized even under homogeneous stress conditions by the fluid start-up inertia, and that such mechanism indeed is present in realistic experimental conditions.

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I. INTRODUCTION

Soft glassy materials (SGMs) present a theoretical concept for fluids that can be solid-like or liquid-like at rest, but all possess a microstructure with strongly interacting building blocks [1]. An extreme class of these are the yield stress fluids, which by virtue of their internal structure behave as solids under an imposed mechanical stress below the yield point, yet flow like fluids once the stress is increased beyond this limit [2–4]. In addition to their extensive utilization in commercial products as, e.g., toothpastes, paints, and process suspensions [5], yield stress fluids are also of profound theoretical interest due to their rich and complex rheological behavior. Indeed, the peculiarities of flow response are also witnessed in shear banding, where the flowing fluid exhibits a spatially banded structure, each band possessing a distinct viscosity associated with a unique shear rate [6]. This banding can appear as a true steady-state structure [7] or as transient shear bands (TSBs), which, while possibly extremely long lived, eventually are replaced by the homogeneous steady state [8]. State-of-the-art observations find transient shear banding of simple yield stress fluids very robustly in different experimental geometries [3]. Furthermore, even though nonthixotropic, such fluids display time- and shear rate or stress-dependent response to step shear, where the relaxation time apparently follows a power law of both applied stress and shear rate [9].

Steady-state shear-banding has been described as a property arising from the nonmonotonic nature of the fluid’s intrinsic flow curve [7,10]. This allows for a mechanically unstable flow regime, where the negative slope in the constitutive curve permits the existence of a nonunique correspondence between shear rates and shear stresses. Thus, in this special regime the fluid may separate into two bands of either identical shear stress (gradient banding) or identical shear rates (vorticity banding) [7]. Such a steady-state scenario is unexpected for fluids known to have monotonic intrinsic flow curves [3].

Against this reasoning, transient shear banding has recently been experimentally observed [3,11] and theoretically predicted even in fluids possessing monotonic flow curves [12]. Numerous reasons for this type of banding have been proposed. In their studies, involving two models, the fluidity model [13] and spatially resolved version of the soft glassy rheology (SGR) model [14], Moorcroft and coworkers [8] predicted transient shear banding resulting from a mechanical instability in the start-up flows. This was clearly seen in the instantaneous (stress-time) constitutive curve as a stress overshoot and subsequent negative slope of the curve as it regresses toward the steady state. In a more recent work, the same authors derive a more rigorous expression for the onset of this mechanical instability in multiple flow scenarios [15].

Transient shear banding in amorphous solids has been successfully modeled by Shi and Falk with shear transformation zone (STZ) theory, in which the plastic deformations occur in specific zones, activated by an effective temperature [16]. At present, Hinkle and Falk are extending this framework to study transient shear banding in simple yield stress fluids (YSF) [17]. These studies properly explain the movement and limited lifetime of the shear bands; however, they leave open detailed origin of the band initiation. To study this aspect, a slightly different approach was proposed in Ref. [18], where a phenomenological, simple scalar \( \phi \) model is utilized. In this case, the local microstructure of a time-dependent fluid is encoded in the \( \phi \) parameter, which refers to the local immobilized volume fraction of the fluid. In the framework of this model, transient shear banding can initiate due to the small stress gradients that are induced by the rotational Couette flow geometry, often utilized in experimental studies. These stress variations generate shear rate heterogeneities, which in turn result in the nonuniform disintegration of the underlying fluid structure, observed as the formation of a TSB [18,19]. However, in experimental geometries, such as the cone-and-plate, where TSB is also found, the stress heterogeneity is considered to be negligible.

In this work, we consider the role of fluid inertia to initiate transient shear bands during the start-up, by solving the Navier-Stokes equations for incompressible flow simultaneously to the evolution of a scalar field variable describing the complex fluid structure. The purpose is to show the effect of accelerating flow to the transient shear band formation, neglected earlier. As reviewed above, to generate transient shear bands, some models preinitialize by hand a nonhomogeneous structure profile [12,17] and others rely on the geometrical stress heterogeneity [12,18]. While especially the latter mechanism compares reasonably to most experimental setups (Couette, parallel plates), its relevance in the shear band initialization may be questioned in others (cone-and-plate). Our results suggest a plausible mechanism initializing transient shear bands even under perfectly...
homogeneous initial conditions due to the flow acceleration mechanism.

Utilizing a computational fluid dynamics (CFD) approach, we apply the $\phi$ model as in Ref. [18] in a homogeneous flow (planar Couette) scenario, where, as mentioned, any and all stress heterogeneities are due to inertial effects alone. We emphasize here that, as will be explained later, the key concept in this model is the fact that the structure breakdown is proportional to the shear rate, a fact based on advanced experiments [3]. Thus, the qualitative behavior shown here is not influenced by this particular model, but is general for all the models and real physical materials that have this property. The paper is organized as follows: in Sec. II we detail the theoretical framework and the implementation. In Sec. III we proceed to comment on the relevant results obtained with our approach, and finally, in Sec. IV, we present our concluding remarks.

II. THE MODEL

As the aim here is to examine TSBs in a time-dependent fluid, a necessary prerequisite for modeling transient shear-banding theoretically involves coupling a structural model describing the internal structure of the fluid to the subsequent flow dynamics. Additionally, as the focus is on providing a minimal example that presents qualitative evidence of transient shear-banding driven by inertial effects, this structural model is chosen from a class of simple phenomenological models based on the abstract scalar structural parameter [5,18,20–23]. The specific $\phi$ model addresses the internal structure of the fluid through the structural parameter $\phi$, describing the immobilized volume fraction present in the fluid [18]. This model allows fine-tuning the fluidization exponent to match the experimental values of various complex fluids, while other similar scalar models (such as the $\lambda$ model by Coussot et al. [19]) inherently produce a fixed fluidization exponent, therefore limiting their applicability for this purpose. Indeed, to the best of our knowledge, the $\phi$ model is the simplest one possessing this crucial feature. Furthermore, the fluidization behavior of more elaborate models, such as the SGR model [24,25], are presently not reported. In the $\phi$ model, the progression of the immobilized volume fraction, $\phi$, in time can be due to shear (constructive and destructive) and shear-independent motion of the structural elements (constructive), reflected in the model as two superimposed kernels. The time- evolution equation for $\phi$ is [18]

$$\frac{d\phi}{dt} = \frac{A_p}{(\mu/\mu_0)^\omega} + (A_r - B_r \phi)(\frac{\dot{\gamma}}{\gamma_0})^k,$$

(1)

where $A_p$ ($B_r$) is a kinetic constant for the shear growth (destruction), $\omega$ is the magnitude of the strain rate (shear rate), and both $k$ and $\gamma_0$ describe the sensitivity of $\phi$ toward shearing. Furthermore, $A_p$, $B_r$, $\omega$, and $\gamma_0$ describe the growth of $\phi$ due to shear-independent effects. Again pursuing a minimal example, setting $A_p = 0$ in Eq. (1) and defining the sample history by fixing the initial immobilized volume fraction $\phi_0$ allows for a minimal inspection of an internally structured fluid with a steady-state $\phi$ of $\phi_m = A_r/B_r$, with the structure breakdown rate set by $B_r$ and proportional to the powers of the dimensionless shear rate ($\dot{\gamma}/\gamma_0)^F$. The proportionality $A_r/B_r$ gives the minimum volume fraction reached by a physical system. For instance, in an aggregating colloidal suspension, this can be thought to describe the monomer volume fraction or in a microgel this could be the volume fraction at the maximally compressed state of the sponglike elements. We define $0 \leq A_i \leq B_i \leq 1$. The parameter $\gamma_0$ determines the system sensitivity to shear; a larger number means longer relaxation time.

The $\phi$ parameter can be incorporated into the flow quantities, as done here, by the empirical Krieger-Dougherty relation [18,19],

$$\eta(\phi) = \eta_0 \left(1 - \frac{\phi}{\phi_m}\right)^{-n},$$

(2)

where $\eta$ is the viscosity of the fluid, $\eta_0$ describes the viscosity of the suspending matrix, and $\phi_m$ denotes the jamming volume fraction, which describes a completely jammed configuration. This gives an additional constraint to the kinetic constants so that $A_r/B_r < \phi_m$. The quantities used in Eq. (2) are set to $\phi_m = 0.68$, $\eta_0 = 1$ mPas (water), and $n = 1.82$ [18].

The final step in the model development is to include Eq. (2) in the Navier-Stokes equations that describe the flow field completely. The incompressible Navier-Stokes equations read

$$\nabla \cdot \mathbf{v} = 0,$$

(3)

and

$$\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v} = -\frac{\nabla p}{\rho} + \nu \nabla^2 \mathbf{v} + \frac{\mathbf{f}}{\rho},$$

(4)

where Eq. (3) is incorporated in the latter equation, physically implying the conservation of momentum. In these equations, $\mathbf{v}$ is the velocity field, $p$ is the pressure, $\rho$ is the density of the fluid, and $\mathbf{f}$ describe bodily forces (e.g., gravity) acting on the fluid (here, $\mathbf{f} = 0$). Additionally, $\nu$ is the kinematic viscosity of the fluid, readily obtained from Eq. (2) applying the relation $\nu = \eta/\rho$. The inertial effects, generally omitted in rheological modeling, which usually deals with creeping flow conditions, are included in the convection and acceleration terms on the left-hand side of Eq. (4).

Transient shear-banding emerges as a property in the fluidization of an internally structured fluid experiencing spatial stress variations and subsequent shear-rate inhomogeneities, leading to spatially nonuniform structural disintegration. As the viscosity is assumed a function of the structural integrity [here modeled by coupling Eqs. (2) and (1)], this is experimentally seen as viscosity bands across the measurement gap. Accordingly, to isolate any sources other than the inertial contributions for such variations, the planar Couette geometry shown in Fig. 1 is utilized in this work. The fluid, confined between the two parallel plates, is subjected to simple shear as the upper plate moves and the lower one remains stationary. In this scenario, the stress is uniform over the gap between the plates, ensuring that all stress variations are due to inertial effects alone.

This approach is implemented in a computational fluid dynamics (CFD) environment. The flexible OpenFOAM software package [26,27] that includes optimized numerical solvers, meshing, and visualization tools is applied and extended to account for the scenario presented here. The simple shear geometry of Fig. 1 is meshed to a 2D 60 $\times$ 60 grid
with periodic boundary conditions at the open boundaries. The practical implementation extends the capabilities of nonNewtonianICOFoam solver to allow for time-dependent viscosity. The system of differential equations is solved using the PCG (PCBiCG) linear solver with DIC (DILU) preconditioning and smoothing, setting the absolute tolerance close to the machine precision of the 64-bit system ($10^{-16}$).

The kernel constants of the $\phi$ model in Eq. (1) were set to $A_k = 0$, $A_s = 0.56$, $B_s = 1.0$, and $\gamma_0 = 1$. Additionally, the gap width $e$ was set to $e = 1.0$ mm. For brevity, the following results refer to the normalized gap (scaled by $1/e$) when necessary. The qualitative results are independent of the selection of these parameters. However, varying the $\gamma_0$ shifts the fluidization curves (see Fig. 4) in the horizontal direction. Changing the ratio $A_s/B_s$ to a smaller value improves the contrast of the shear band edge, i.e., makes the kink in the velocity profile steeper, and shifts the fluidization curves in the vertical direction having similar effect as increasing the $\phi_0$ (Fig. 4).

III. RESULTS

The Navier-Stokes equation is characterized (at steady state) by the Reynolds number, which is represented here by the shear rate. In addition in the relaxation of the model depends on the shear rate exponent $k$ and the initial condition $\phi_0$. Thus, this set of parameters define the TSB and is studied in what follows. In Fig. 2 ($\phi_0 = 0.67999$, $\dot{\gamma} = 0.2$ 1/s), the linear velocity profile is displayed in the homogeneous, planar Couette start-up flow scenario. In experiments, these 1D pictures are accessed by, e.g., ultrasonic speckle velocimetry [3] and, in general, are used to identify shear localization effects. Observing the evolution of the velocity in the flow direction allows us to monitor the shear localization here as well. As demonstrated in the example scenario of Fig. 2, shear banded flow profile develops in the course of a few seconds from the onset of the flow. Here we emphasize that no external initial disturbance to the model is required and the shear localization is induced by the stress inhomogeneity due to the initial acceleration of the fluid, which interacts with the viscosity evolution as discussed in detail for the creeping flow case in Ref. [18].

With these model parameters, the TSB persists for up until $t \approx 300$ s, when complete fluidization and the steady-state flow profile is reached. This certainly is a timescale comparable to the experiments, where long-lasting transient banding was observed [3]. Note that since the mechanism here is based on the flow model interaction with the time-dependent shear thinning of the fluid, any model having this property will potentially experience shear banding induced by the same effect. Experimentally, this behavior is present in systems showing microstructural disintegration due to shear, where the time-dependence is a power law (typically of exponents in the range of 2–4) of the shear rate or shear stress [3]. Conversely, if the structural decomposition is linear (power-law exponent $k \approx 1.0$), the inertial effects and the subsequent stress variations are incapable of generating a TSB. This is illustrated in Fig. 3, where the model parameters are identical to those in Fig. 2 aside from the exponent of the $\phi$ model ($k = 1.0$). Here, due to the linear dependence between $\phi$ and $\dot{\gamma}$, the structural breakdown is uniform and the shear localization does not
The fluidization time decays rapidly by increasing the applied shear rate. We have resorted to the applied shear rate to quantify the fluidization times, as seen in Fig. 3, since it is this quantity that provides the necessary stress heterogeneity in the beginning of the flow. This point is illustrated in Fig. 4, where the fluidization time \( \tau_f \) (here, the time the TSB persists) is represented as a function of the applied shear rate \( \langle \gamma' \rangle \). For each \( \langle \gamma' \rangle \), \( \tau_f \) was determined from the linear velocity profile (as shown in Fig. 2) as follows: two separate linear curves were fitted to the data, one spanning the area \( 0 \leq r/e \leq 0.33 \), and the other \( 0.66 \leq r/e \leq 1.0 \).

The slopes \( a_1 \) and \( a_2 \) of these curves reached a certain threshold (here: \(|a_1 - a_2|/a_2 \leq 5.0 \cdot 10^{-2}\)), the profile was determined to having reached the homogeneous flow state. The results are displayed in Fig. 4, where it is observed that a sufficient value of \( \langle \gamma' \rangle \) (and accordingly, sufficient stress heterogeneity) is required for transient shear banding, otherwise an uniform breakdown of the underlying structure is witnessed (\( \tau_f = 0 \)). Once this \( \langle \gamma' \rangle \) is reached, the time required for complete fluidization decays rapidly. Moreover, if the structural decomposition is linear (\( k = 1.0 \)), the breakdown is uniform regardless of \( \langle \gamma' \rangle \). Note that the discrete ramp in the fluidization times should not be interpreted literally as the transformation from strong shear localization (TSB) to homogeneous flow is of continuous nature. However, to quantify the fluidization times, we have resorted to the procedure introduced above, which essentially imposes a cut-off criterion (and the discrete jump) to the results.

Additionally, a complementing point of view on TSB formation is provided by various temporal plots. In Fig. 5, the apparent shear stress \( \sigma_a \), measured at the shearing plane, is displayed as a function of time \( t \) for various applied shear rates \( \langle \gamma' \rangle \). As the flow progresses with increasing time, the microstructure of the fluid disintegrates and the local jammed volume fraction at the shearing plane decreases, leading to a monotonic decrease of the effective viscosity as well, as the two are linked by Eq. (2). This, in turn, leads to a monotonic decrease in the shear stress, as observed in the figure. Furthermore, the time at which the stresses reach their steady-state values seems to concur well with the fluidization time observed in Fig. 4 as one would expect.

\[
\sigma_a(t) = \rho w^2/\eta (w \text{ denoting the gap width}), \text{ as for a simple (Newtonian) liquid.}
\]

Judging by this expression, the high viscosity of the jammed initial configuration should yield an extremely low fluidization time. Indeed, as seen in Fig. 3, the initial fluidization occurs within \( 10^{-10} \) seconds from the moment the flow commences. The results are displayed in Fig. 4, where it is observed that a sufficient value of \( \langle \gamma' \rangle \) (and accordingly, sufficient stress heterogeneity) is required for transient shear banding, otherwise an uniform breakdown of the underlying structure is witnessed (\( \tau_f = 0 \)). Once this \( \langle \gamma' \rangle \) is reached, the time required for complete fluidization decays rapidly. Moreover, if the structural decomposition is linear (\( k = 1.0 \)), the breakdown is uniform regardless of \( \langle \gamma' \rangle \). Note that the discrete ramp in the fluidization times should not be interpreted literally as the transformation from strong shear localization (TSB) to homogeneous flow is of continuous nature. However, to quantify the fluidization times, we have resorted to the procedure introduced above, which essentially imposes a cut-off criterion (and the discrete jump) to the results.

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\]
Another temporal plot is illustrated in Fig. 6, where the shear band edge is tracked over the normalized gap ($\delta/e$) as a function of time $t$. In this plot, the value $\delta/e = 0$ corresponds to a scenario where the flow is completely localized in the region near the shearing plane and $\delta/e = 1$ where the TSB vanishes. For consistency, the shear band edge $\delta$ was determined by the linear fitting scheme introduced earlier (see the commentary on Fig. 4). The edge location was determined as the intersection point of the two linear curves as long as the steady-state condition ($\langle a_1 - a_2 \rangle/a_2 \leq 10^{-2}$) was not met. In the framework of the $\phi$ model, the shear band edge travels at a varying (nonconstant) velocity, dependent on the applied shear rate ($\dot{\gamma}$). In addition, the fluidization process is gradual up to a critical point, at which the fluid suddenly yields completely. This is observed in Fig. 6 as the discrete jump of the edge location to the value $\delta/e = 1$. The exact location of this jump is dependent on the applied shear ($\dot{\gamma}$). The behavior witnessed here should be compared with the corresponding earlier results [18], where the shear band edge also proceeds in a highly nonlinear manner. However, the critical point is not observed, and the edge travels independent of the applied shear rate ($\dot{\gamma}$) for all $k$. The reason for these differences lies in the fundamentally different source of the stress gradient, which serves as the catalyst for transient shear banding. In Ref. [18], this stress variation is induced by the geometry and is essentially time-independent. Here, the stress variation is a (time-dependent) result of the finite fluid inertia, which is directly influenced by ($\dot{\gamma}$). This leads to a weaker localization of the fluid flow at low ($\dot{\gamma}$) and strong localization at high ($\dot{\gamma}$).

Indeed, the blue curve in Fig. 6 ($\langle \dot{\gamma} \rangle = 10 \text{s}^{-1}$) bears a strong resemblance to the results in Ref. [18], while lower values of ($\dot{\gamma}$) yield a more convoluted profile: the velocity of the shear band edge increases at first, but then decreases, and finally diverges as the critical point is reached. Thus, rather than reaching the static plate, the shear band disperses suddenly as the stress gradient has diminished over time and is unable to sustain the banded profile.

Finally, Fig. 7 provides a semilogarithmic “phase” diagram, in which the regions of localized and uniform shear are displayed. The boundary indicates the minimum triggering value of ($\dot{\gamma}$), at each $k$ required to yield significant heterogeneous structure relaxation, triggered by the start-up stress overshoot due to the fluid inertia. Above this value, a TSB forms, and below it the coupling between the structure relaxation and the local shear heterogeneity during the start-up inertia is not strong enough to trigger the TSB. At this regime the structure relaxes homogeneously, manifested by uniform shear. The boundary between these two regimes moves to lower shear rates, as the relaxation exponent is increased. As Ref. [18] explains, in the framework of this model, a kinetic exponent on the order of $k \sim 2$ would be required to match the duration of the TSB to experiments. Unfortunately, using here an exponent as high as this would not be permitted due to numerical and computational limitations (the number of required iterations for convergence). Extrapolating the monotonically decreasing trend based on the computed values of Fig. 6 to $k = 2$ hints that the minimum value for ($\dot{\gamma}$) should be well below the typical (minimum) experimentally used shear rates ($\langle \dot{\gamma} \rangle \sim 10^{-2}$).

Therefore, we are inclined to argue based on the model, TSB formation and the subsequent localized flow dynamics due to start-up inertia only should be recovered trivially for all real-world complex fluids. This has the important implication for the experiments that TSB should appear in all simple yield stress fluids with such fluidization exponents irrespective of the measuring geometry.

**IV. CONCLUSIONS**

Earlier theoretical work proposes a scenario where the transient shear banding is initialized by gradients in stress [18] or inhomogeneity of the sample [12,17,24]. The present study brings a new mechanism, which shows that transient shear banding can result even due to the start-up stress gradients caused by accelerating flow. As we show here, depending on the linearity of the fluids’ viscosity response, and its initial state, this effect can be either negligible or very significant. When the initial viscosity of the fluid is small, and/or the time-dependence of the fluid is close to linear, the stress gradient is not able to induce any inhomogeneities during the start-up flow. However, according to our simulations, when the fluid at rest is in a high-viscosity state and shows time dependence under constant shear rate with a large fluidization exponent, the start-up stress inhomogeneities initialize long-lasting transient shear bands at all experimentally accessible shear rates. This occurs despite the fact that the influence of the Navier-Stokes instability is multiple orders of magnitude faster compared to the actual TSB. However, it creates a small but nonnegligible inhomogeneity in the structure, which is amplified over time into a complete TSB. An example of such material is the carbopol, a typical example of so-called simple yield stress fluids, for which the fluidization exponent is larger than 2 [3] and

![Fig. 7. Planar Couette start-up flow: a semilogarithmic phase diagram that classifies the flow as either uniform or localized (a TSB is formed). The boundary is defined by the minimum (triggering) value of the applied shear rate ($\dot{\gamma}$) (dependent on $k$), above which the start-up inertia induces a TSB and the corresponding banded profile is retrieved. Below this value, the flow remains decidedly uniform. As seen here, this value declines rapidly as a function of $k$. Note that the $k$ values for real-world complex fluids are on the order of $k \sim 2$ as easily verified in Ref. [18]. Therefore, extrapolating the minimum value for ($\dot{\gamma}$) using this $k$ suggests that shear localization should occur trivially due to the start-up inertia for any real complex fluids in the experimentally accessible shear rates [typically ($\dot{\gamma}$)$_{\text{min}} \sim 10^{-2}$ (1/s)].](image-url)
the viscosity diverges at rest. Our findings give a reasonable explanation for the initialization of transient shear banding even in experimental geometries exhibiting negligible stress heterogeneities, such as the cone and plate one. This suggests that stress heterogeneities should be anticipated in all strongly shear thinning fluids during the start-up phase of rheological experiments.

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